# PRINCIPLES OF ECONOMICS <br> for non-economists 

Xavier Martinez-Giralt

January 2008

Copyright (c) 2008 Xavier Martinez-Giralt.
Permission is granted to copy, distribute and/or modify this document under the terms of the GNU Free Documentation License, Version 1.2 or any later version published by the Free Software Foundation; with the Invariant Sections, with the Front-Cover Texts, and with the Back-Cover Texts. A copy of the license is included in the section entitled "GNU Free Documentation License".

## PRINCIPLES OF ECONOMICS

## 1. Economics. What is this?

## 2. The agents of the economy

2.1 Demand: consumers, patients, elasticity
2.2 Supply: firms, hospitals physicians;
Efficiency, Efficacy, Effectiveness, Equity,
Opportunity cost
3. The market
3.1 Definition
3.2 Market structures
3.3 Perfectly competitive markets
4. Sources of market failure
4.1 Oligopoly
4.2 Monopoly
5. R\&D and technology transfer
5.1 R\&D
5.2 Patents
5.3 Licenses
6. Externalities
7. Merit goods
8. Uncertainty, risk and insurance
8.1 Attitudes towards risk
8.2 Insurance market

## 9. Contract theory

9.1 Contracts, information and agency relation
9.2 Adverse selection, moral hazard and signalling

## 10. Pricing

10.1 Price discrimination
10.2 Ramsey pricing

## 11. Macroeconomics

11.1 What is macroeconomics about?
11.2 The working of the economy
11.3 Macroeconomics of the health sector

## References

Cabral, L., 2000, Introduction to Industrial Organization, Cambridge (Mass.), The MIT Press.
Carlton, D.W., and J.M. Perloff, 2005, Modern Industrial Organization, Boston, Pearson.
Hay, D.A., and D.J. Morris, 1996, Industrial Economics and Organization, New York, Oxford University Press.
McEachern, W.A., 1997, Economics. A Contemporary Introduction, Cincinnati (Ohio), South-Western College Publishing Co.
Salvatore, D., 2003, Microeconomics. Theory and Applications, Oxford, Oxford University Press.
Shy, O., 1995, Industrial Organization, Cambridge (Mass.), The MIT Press.

# GNU Free Documentation License 

Version 1.2, November 2002
Copyright © $2000,2001,2002$ Free Software Foundation, Inc.
59 Temple Place, Suite 330, Boston, MA 02111-1307 USA
Everyone is permitted to copy and distribute verbatim copies of this license
document, but changing it is not allowed.

## Preamble

The purpose of this License is to make a manual, textbook, or other functional and useful document "free" in the sense of freedom: to assure everyone the effective freedom to copy and redistribute it, with or without modifying it, either commercially or noncommercially. Secondarily, this License preserves for the author and publisher a way to get credit for their work, while not being considered responsible for modifications made by others.

This License is a kind of "copyleft", which means that derivative works of the document must themselves be free in the same sense. It complements the GNU General Public License, which is a copyleft license designed for free software.

We have designed this License in order to use it for manuals for free software, because free software needs free documentation: a free program should come with manuals providing the same freedoms that the software does. But this License is not limited to software manuals; it can be used for any textual work, regardless of subject matter or whether it is published as a printed book. We recommend this License principally for works whose purpose is instruction or reference.

## 1 Applicability and Definitions

This License applies to any manual or other work, in any medium, that contains a notice placed by the copyright holder saying it can be distributed under the terms
of this License. Such a notice grants a world-wide, royalty-free license, unlimited in duration, to use that work under the conditions stated herein. The 'Document", below, refers to any such manual or work. Any member of the public is a licensee, and is addressed as "you". You accept the license if you copy, modify or distribute the work in a way requiring permission under copyright law.

A "Modified Version" of the Document means any work containing the Document or a portion of it, either copied verbatim, or with modifications and/or translated into another language.

A "Secondary Section" is a named appendix or a front-matter section of the Document that deals exclusively with the relationship of the publishers or authors of the Document to the Document's overall subject (or to related matters) and contains nothing that could fall directly within that overall subject. (Thus, if the Document is in part a textbook of mathematics, a Secondary Section may not explain any mathematics.) The relationship could be a matter of historical connection with the subject or with related matters, or of legal, commercial, philosophical, ethical or political position regarding them.

The 'Invariant Sections" are certain Secondary Sections whose titles are designated, as being those of Invariant Sections, in the notice that says that the Document is released under this License. If a section does not fit the above definition of Secondary then it is not allowed to be designated as Invariant. The Document may contain zero Invariant Sections. If the Document does not identify any Invariant Sections then there are none.

The "Cover Texts" are certain short passages of text that are listed, as FrontCover Texts or Back-Cover Texts, in the notice that says that the Document is released under this License. A Front-Cover Text may be at most 5 words, and a Back-Cover Text may be at most 25 words.

A "Transparent" copy of the Document means a machine-readable copy, represented in a format whose specification is available to the general public, that is suitable for revising the document straightforwardly with generic text editors or (for images composed of pixels) generic paint programs or (for drawings) some widely available drawing editor, and that is suitable for input to text formatters or for automatic translation to a variety of formats suitable for input to text formatters. A copy made in an otherwise Transparent file format whose markup, or absence of markup, has been arranged to thwart or discourage subsequent modification by readers is not Transparent. An image format is not Transparent if used for any substantial amount of text. A copy that is not "Transparent" is called "Opaque".

Examples of suitable formats for Transparent copies include plain ASCII without markup, Texinfo input format, LaTeX input format, SGML or XML using a publicly available DTD, and standard-conforming simple HTML, PostScript or PDF designed for human modification. Examples of transparent image formats include PNG, XCF and JPG. Opaque formats include proprietary formats that can be read and edited only by proprietary word processors, SGML or XML for which the DTD and/or processing tools are not generally available, and the machinegenerated HTML, PostScript or PDF produced by some word processors for output
purposes only.
The 'Title Page" means, for a printed book, the title page itself, plus such following pages as are needed to hold, legibly, the material this License requires to appear in the title page. For works in formats which do not have any title page as such, "Title Page" means the text near the most prominent appearance of the work's title, preceding the beginning of the body of the text.

A section 'Entitled XYZ' means a named subunit of the Document whose title either is precisely XYZ or contains XYZ in parentheses following text that translates XYZ in another language. (Here XYZ stands for a specific section name mentioned below, such as "Acknowledgements", 'Dedications", ''Endorsements", or "History".) To "Preserve the Title" of such a section when you modify the Document means that it remains a section "Entitled XYZ" according to this definition.

The Document may include Warranty Disclaimers next to the notice which states that this License applies to the Document. These Warranty Disclaimers are considered to be included by reference in this License, but only as regards disclaiming warranties: any other implication that these Warranty Disclaimers may have is void and has no effect on the meaning of this License.

## 2 Verbatim Copying

You may copy and distribute the Document in any medium, either commercially or noncommercially, provided that this License, the copyright notices, and the license notice saying this License applies to the Document are reproduced in all copies, and that you add no other conditions whatsoever to those of this License. You may not use technical measures to obstruct or control the reading or further copying of the copies you make or distribute. However, you may accept compensation in exchange for copies. If you distribute a large enough number of copies you must also follow the conditions in section 3 .

You may also lend copies, under the same conditions stated above, and you may publicly display copies.

## 3 Copying in Quantity

If you publish printed copies (or copies in media that commonly have printed covers) of the Document, numbering more than 100, and the Document's license notice requires Cover Texts, you must enclose the copies in covers that carry, clearly and legibly, all these Cover Texts: Front-Cover Texts on the front cover, and BackCover Texts on the back cover. Both covers must also clearly and legibly identify you as the publisher of these copies. The front cover must present the full title with all words of the title equally prominent and visible. You may add other material on the covers in addition. Copying with changes limited to the covers, as long as they
preserve the title of the Document and satisfy these conditions, can be treated as verbatim copying in other respects.

If the required texts for either cover are too voluminous to fit legibly, you should put the first ones listed (as many as fit reasonably) on the actual cover, and continue the rest onto adjacent pages.

If you publish or distribute Opaque copies of the Document numbering more than 100, you must either include a machine-readable Transparent copy along with each Opaque copy, or state in or with each Opaque copy a computer-network location from which the general network-using public has access to download using public-standard network protocols a complete Transparent copy of the Document, free of added material. If you use the latter option, you must take reasonably prudent steps, when you begin distribution of Opaque copies in quantity, to ensure that this Transparent copy will remain thus accessible at the stated location until at least one year after the last time you distribute an Opaque copy (directly or through your agents or retailers) of that edition to the public.

It is requested, but not required, that you contact the authors of the Document well before redistributing any large number of copies, to give them a chance to provide you with an updated version of the Document.

## 4 Modifications

You may copy and distribute a Modified Version of the Document under the conditions of sections 2 and 3 above, provided that you release the Modified Version under precisely this License, with the Modified Version filling the role of the Document, thus licensing distribution and modification of the Modified Version to whoever possesses a copy of it. In addition, you must do these things in the Modified Version:
A. Use in the Title Page (and on the covers, if any) a title distinct from that of the Document, and from those of previous versions (which should, if there were any, be listed in the History section of the Document). You may use the same title as a previous version if the original publisher of that version gives permission.
B. List on the Title Page, as authors, one or more persons or entities responsible for authorship of the modifications in the Modified Version, together with at least five of the principal authors of the Document (all of its principal authors, if it has fewer than five), unless they release you from this requirement.
C. State on the Title page the name of the publisher of the Modified Version, as the publisher.
D. Preserve all the copyright notices of the Document.
E. Add an appropriate copyright notice for your modifications adjacent to the other copyright notices.
F. Include, immediately after the copyright notices, a license notice giving the public permission to use the Modified Version under the terms of this License, in the form shown in the Addendum below.
G. Preserve in that license notice the full lists of Invariant Sections and required Cover Texts given in the Document's license notice.
H. Include an unaltered copy of this License.
I. Preserve the section Entitled "History", Preserve its Title, and add to it an item stating at least the title, year, new authors, and publisher of the Modified Version as given on the Title Page. If there is no section Entitled "History" in the Document, create one stating the title, year, authors, and publisher of the Document as given on its Title Page, then add an item describing the Modified Version as stated in the previous sentence.
J. Preserve the network location, if any, given in the Document for public access to a Transparent copy of the Document, and likewise the network locations given in the Document for previous versions it was based on. These may be placed in the "History" section. You may omit a network location for a work that was published at least four years before the Document itself, or if the original publisher of the version it refers to gives permission.
K. For any section Entitled "Acknowledgements" or "Dedications", Preserve the Title of the section, and preserve in the section all the substance and tone of each of the contributor acknowledgements and/or dedications given therein.
L. Preserve all the Invariant Sections of the Document, unaltered in their text and in their titles. Section numbers or the equivalent are not considered part of the section titles.
M. Delete any section Entitled "Endorsements". Such a section may not be included in the Modified Version.
N. Do not retitle any existing section to be Entitled "Endorsements" or to conflict in title with any Invariant Section.
O. Preserve any Warranty Disclaimers.

If the Modified Version includes new front-matter sections or appendices that qualify as Secondary Sections and contain no material copied from the Document, you may at your option designate some or all of these sections as invariant. To do this, add their titles to the list of Invariant Sections in the Modified Version's license notice. These titles must be distinct from any other section titles.

You may add a section Entitled "Endorsements", provided it contains nothing but endorsements of your Modified Version by various parties-for example, statements of peer review or that the text has been approved by an organization as the authoritative definition of a standard.

You may add a passage of up to five words as a Front-Cover Text, and a passage of up to 25 words as a Back-Cover Text, to the end of the list of Cover Texts in the Modified Version. Only one passage of Front-Cover Text and one of Back-Cover Text may be added by (or through arrangements made by) any one entity. If the Document already includes a cover text for the same cover, previously added by you or by arrangement made by the same entity you are acting on behalf of, you may not add another; but you may replace the old one, on explicit permission from the previous publisher that added the old one.

The author(s) and publisher(s) of the Document do not by this License give permission to use their names for publicity for or to assert or imply endorsement of any Modified Version.

## 5 Combining Documents

You may combine the Document with other documents released under this License, under the terms defined in section 4 above for modified versions, provided that you include in the combination all of the Invariant Sections of all of the original documents, unmodified, and list them all as Invariant Sections of your combined work in its license notice, and that you preserve all their Warranty Disclaimers.

The combined work need only contain one copy of this License, and multiple identical Invariant Sections may be replaced with a single copy. If there are multiple Invariant Sections with the same name but different contents, make the title of each such section unique by adding at the end of it, in parentheses, the name of the original author or publisher of that section if known, or else a unique number. Make the same adjustment to the section titles in the list of Invariant Sections in the license notice of the combined work.

In the combination, you must combine any sections Entitled "History" in the various original documents, forming one section Entitled "History"; likewise combine any sections Entitled "Acknowledgements", and any sections Entitled "Dedications". You must delete all sections Entitled "Endorsements".

## 6 Collections of Documents

You may make a collection consisting of the Document and other documents released under this License, and replace the individual copies of this License in the various documents with a single copy that is included in the collection, provided that you follow the rules of this License for verbatim copying of each of the documents in all other respects.

You may extract a single document from such a collection, and distribute it individually under this License, provided you insert a copy of this License into the extracted document, and follow this License in all other respects regarding verbatim copying of that document.

## 7 Aggregation With Independent Works

A compilation of the Document or its derivatives with other separate and independent documents or works, in or on a volume of a storage or distribution medium, is called an "aggregate" if the copyright resulting from the compilation is not used to limit the legal rights of the compilation's users beyond what the individual works permit. When the Document is included in an aggregate, this License does not apply to the other works in the aggregate which are not themselves derivative works of the Document.

If the Cover Text requirement of section 3 is applicable to these copies of the Document, then if the Document is less than one half of the entire aggregate, the Document's Cover Texts may be placed on covers that bracket the Document within the aggregate, or the electronic equivalent of covers if the Document is in electronic form. Otherwise they must appear on printed covers that bracket the whole aggregate.

## 8 Translation

Translation is considered a kind of modification, so you may distribute translations of the Document under the terms of section 4. Replacing Invariant Sections with translations requires special permission from their copyright holders, but you may include translations of some or all Invariant Sections in addition to the original versions of these Invariant Sections. You may include a translation of this License, and all the license notices in the Document, and any Warranty Disclaimers, provided that you also include the original English version of this License and the original versions of those notices and disclaimers. In case of a disagreement between the translation and the original version of this License or a notice or disclaimer, the original version will prevail.

If a section in the Document is Entitled "Acknowledgements", "Dedications", or "History", the requirement (section 4) to Preserve its Title (section 1) will typically require changing the actual title.

## 9 Termination

You may not copy, modify, sublicense, or distribute the Document except as expressly provided for under this License. Any other attempt to copy, modify, sublicense or distribute the Document is void, and will automatically terminate your
rights under this License. However, parties who have received copies, or rights, from you under this License will not have their licenses terminated so long as such parties remain in full compliance.

## 10 Future Revisions of This License

The Free Software Foundation may publish new, revised versions of the GNU Free Documentation License from time to time. Such new versions will be similar in spirit to the present version, but may differ in detail to address new problems or concerns. See http://www.gnu.org/copyleft/.

Each version of the License is given a distinguishing version number. If the Document specifies that a particular numbered version of this License "or any later version" applies to it, you have the option of following the terms and conditions either of that specified version or of any later version that has been published (not as a draft) by the Free Software Foundation. If the Document does not specify a version number of this License, you may choose any version ever published (not as a draft) by the Free Software Foundation.

## PRINCIPLES OF ECONOMICS

## 1. Economics. What is this?



Economics: Study of the way in which economic agents take their decisions regarding the use (allocation) of scarce resources.

Economic agents: Decision makers in the economy. Individuals, households, enterprises (for profit, nonprofit; production, distribution), State.

## Decisions:

- what to produce/consume?
- how much to produce/consume?
- How to produce/consume?
- Who produces/consumes?

Answers to these questions depend on the organization of the economy: central plan, free market, mixed systems.

Reality too complex. Study of an economy by means of models (theories): set of assumptions providing a simplified representation of reality capturing the fundamental relationships among economic agents [ $\rightarrow$ road map vs. road network].

Two (complementary) uses of models:

- description of decision making process $\rightarrow$ positive economics
- policy design (control and improvement of decision making) $\rightarrow$ normative economics
$\star$ Resources: inputs, factors of production.
- land (physical resources of the planet)
- labor (human resources)
- capital (resources created by human to aid in production: tools, machinery, factories, ...)
enterprise: organization of resources to produce goods and services.
$\star$ Main concepts related with scarcity:


## Efficiency

Opportunity cost

Production Possibility Frontier

## 2. The agents of the economy

## Population (Demand)



3D consumption set


Individual vs. aggregate demand

## Individual demand $\rightarrow$ solution of

$$
\begin{gathered}
\max _{x, y} U(x, y) \text { s.t. } M=P_{x} x+P_{y} y \\
x^{*}\left(P_{x}, P_{y}, M\right) \\
y^{*}\left(P_{x}, P_{y}, M\right)
\end{gathered}
$$






Consider 2 individuals $x_{1}\left(P_{x}, P_{y}, M_{1}\right)$ and $x_{2}\left(P_{x}, P_{y}, M_{2}\right)$.

The aggregate (market) demand for good $x$ is the horizontal sum of individual demands.


## Effects on (aggregate) demand

Changes along the demand curve [( $\left.P_{y}, M\right)$ given]

- $\uparrow P_{x}, x \downarrow$ : some consumers buy less and some others leave the market.
- $\downarrow P_{x}, x \uparrow$ : some consumers buy more and some others enter the market.



Shifting the demand curve [ $\left(P_{x}, P_{y}\right)$ given]

- $\uparrow M \longrightarrow$ increase demand $x$ and $y$ : demand curve moves outwards.


## Crossed effects [( $\left.P_{x}, M\right)$ given]

Impact of $\uparrow P_{y}$ ( $M$ constant) on $x$, three possibilities:
(i) $x$ and $y$ independent, e.g. ( $\mathrm{x}, \mathrm{y}$ ) = (coffee, gasoline):
$\uparrow P_{y} \rightarrow \downarrow y \rightarrow$ demand of $x$ unaffected
(ii) $x$ and $y$ substitutes: satisfy similar needs, e.g. ( $\mathrm{x}, \mathrm{y}$ ) $=$ (butter, margarine):
$\uparrow P_{y} \rightarrow \downarrow$ demand of $y \rightarrow \uparrow$ demand of $x$.
(iii) $x$ and $y$ complements: joint consumption, e.g.
( $\mathrm{x}, \mathrm{y}$ ) = (coffe, sugar):
$\uparrow P_{y} \rightarrow \downarrow$ demand of $y \rightarrow \downarrow$ demand of $x$.

$(x, y)$ substitutes

$(x, y)$ complements

Elasticity

How to measure the impact of $\Delta P_{x}$ on $x$ ?

Method 1: Direct and simple

$$
\frac{\Delta x}{\Delta P_{x}}
$$

Problem: dependent on units

| EURO |  | Peseta |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}_{\mathrm{x}}$ | x | $\mathrm{P}_{\mathrm{x}}$ | x |
| 6 | 10 | 1000 | 10 |
| 12 | 5 | 2000 | 5 |

$$
\begin{aligned}
& \left.\frac{\Delta x}{\Delta P_{x}}\right|_{E U R}=\frac{-5}{6}=-0.83 \\
& \left.\frac{\Delta x}{\Delta P_{x}}\right|_{P t s}=\frac{-5}{1000}=-0.005
\end{aligned}
$$

Method 2: Index invariant to units $\longrightarrow$
Elasticity

Own-price elasticity

$$
\left|\varepsilon_{x}\right|=\left|\frac{\% \Delta x}{\% \Delta P_{x}}\right|=\left|\frac{\frac{\Delta x}{x}}{\frac{\Delta P_{x}}{P_{x}}}\right|=\left|\frac{\Delta x P_{x}}{\Delta P_{x} x}\right|
$$

$\left|\varepsilon_{x}\right|>1$ elastic (overreaction)
$\left|\varepsilon_{x}\right|<1$ inelastic (underreaction)
Example: $\left|\varepsilon_{x}\right|=\frac{1}{2}$
Cross-price elasticity

$$
\varepsilon_{x y}=\frac{\% \Delta x}{\% \Delta P_{y}}=\frac{\frac{\Delta x}{x}}{\frac{\Delta P_{y}}{P_{y}}}=\frac{\Delta x P_{y}}{\Delta P_{y} x}
$$

Income elasticity

$$
\eta_{x}=\frac{\% \Delta x}{\% \Delta M}=\frac{\frac{\Delta x}{x}}{\frac{\Delta M}{M}}=\frac{\Delta x M}{\Delta M x}
$$

## Ilustration

## Derivation of the demand function

- Consider a two-good economy: a composite consumption good $(y)$ and health care $(x)$.
- (Representative) individual's utility function:

$$
U(x, y)=x^{\alpha} y^{\beta}, \alpha, \beta>0
$$

- Individual's income $m$.
- Individual's budget constraint:

$$
m \geq x P_{x}+y P_{y}
$$

where $P_{x}$ y $P_{y}$ denote prices of $x$ and $y$ respectively.

- Individual's problem:

Select a bundle $(x, y)$ to maximize utility given $\left(P_{x}, P_{y} ; m\right)$ :

$$
\max _{x, y} x^{\alpha} y^{\beta} \text { s.t. } m \geq x P_{x}+y P_{y}
$$

## Solution:

$$
\max _{x, y} L(x, y)=x^{\alpha} y^{\beta}+\lambda\left(m-x P_{x}-y P_{y}\right)
$$

First order conditions,

$$
\begin{align*}
& \frac{\partial L}{\partial x}=\alpha x^{\alpha-1} y^{\beta}-\lambda P_{x}=0  \tag{1}\\
& \frac{\partial L}{\partial y}=\beta y^{\beta-1} x^{\alpha}-\lambda P_{y}=0  \tag{2}\\
& \frac{\partial L}{\partial \lambda}=m-x P_{x}+y P_{y}=0 \tag{3}
\end{align*}
$$

From (1) and (2),

$$
\frac{\alpha y}{\beta x}=\frac{P_{x}}{P_{y}}
$$

That is,

$$
\begin{equation*}
y=\frac{\beta x}{\alpha} \frac{P_{x}}{P_{y}} \tag{4}
\end{equation*}
$$

Substituting (4) in (3) yields

$$
\begin{equation*}
x\left(P_{x}, m\right)=\frac{\alpha m}{P_{x}(\alpha+\beta)} \tag{5}
\end{equation*}
$$

Substituting (5) in (4) yields

$$
\begin{equation*}
y\left(P_{y}, m\right)=\frac{\beta m}{P_{y}(\alpha+\beta)} \tag{6}
\end{equation*}
$$

Example Society with two consumers $a$ and $b$ and two goods $x$ and $y$.

$$
\begin{aligned}
U_{a}\left(x_{a}, y_{a}\right) & =x_{a}^{\frac{1}{3}} y_{a}^{\frac{2}{3}} \\
U_{b}\left(x_{b}, y_{b}\right) & =x_{b}^{\frac{2}{3}} y_{b}^{\frac{1}{3}}
\end{aligned}
$$

Individual demands:

$$
\begin{aligned}
x_{a}\left(P_{x}, m\right) & =\frac{m}{3 P_{x}} \\
y_{a}\left(P_{y}, m\right) & =\frac{2 m}{3 P_{y}} \\
x_{b}\left(P_{x}, m\right) & =\frac{2 m}{3 P_{x}} \\
y_{b}\left(P_{y}, m\right) & =\frac{m}{3 P_{y}}
\end{aligned}
$$

Market demands:

$$
\begin{aligned}
x\left(P_{x}, m\right) & =\frac{m}{P_{x}} \\
y\left(P_{y}, m\right) & =\frac{m}{P_{y}}
\end{aligned}
$$



Elasticity
$\diamond$ own-price elasticity

$$
\begin{aligned}
\varepsilon_{x_{a}} & =\frac{\partial x_{a}}{\partial P_{x}} \frac{P_{x}}{x_{a}}=-\frac{1}{3} \\
\varepsilon_{x_{b}} & =\frac{\partial x_{b}}{\partial P_{x}} \frac{P_{x}}{x_{a}}=-\frac{2}{3} \\
\varepsilon_{x} & =\frac{\partial x}{\partial P_{x}} \frac{P_{x}}{x_{a}}=-1
\end{aligned}
$$

$\diamond$ income elasticity

$$
\begin{aligned}
\eta_{x_{a}} & =\frac{\partial x_{a}}{\partial m} \frac{m}{x_{a}}=1 \\
\eta_{x_{b}} & =\frac{\partial x_{b}}{\partial m} \frac{m}{x_{a}}=1 \\
\eta_{x} & =\frac{\partial x}{\partial m} \frac{m}{x_{a}}=1
\end{aligned}
$$

## Producers (Suppliers).



$$
\begin{aligned}
& C(x)=F+V(x) \\
& A C(x)=\frac{C(x)}{x} \\
& M C(x)=\frac{\partial C(x)}{\partial x}
\end{aligned}
$$



## Production function

© relation between output and inputs: output = f (inputs).
$\rightarrow$ engineering approach to prduction activity.
© Def.: represents the maximum amount of output that can be obtained from a given combination of inputs. (conveys efficiency)

- Graphical representation (1 output, 2 inputs):
(a) isoquant map $\rightarrow$ degree of substitutability of inputs.
(b) 3 D
(c) Production possibility frontier


## (a) isoquant map


(b) 3D representation


Consider an enterprise producing hardware and software. If all engineers produce hardware $\rightarrow 50$ units/week; If all inputs to software $\rightarrow 50$ units/week.


Points $A, B, C \in$ feasible production set. Represent production of firm (supply). Points $B, C \in \mathrm{FPP}$.

## Production possibility frontier:

Set of all the maximum combinations of production levels the firm can achieve given the quantity and productivity of resources available.

## Efficiency.

An allocation of resources is efficient if it is impossible to change that allocation to make an agent better off (increase utility/profit) without making another agent worse off (reduce utility/profit).

Efficiency refers to allocations of resources yielding the maximum possible output, i.e. allocations on PPF.

Hence, allocation $A$ is not efficient, while allocations $B, C$ are efficient.

From a social point of view, there is interest in moving from $A$ to $B$ (or $C$ ). The firm is able to increase its output with the same inputs.

## Efficacy.

Potential benefit of a technology. Probability that an individual benefits from the application of a (health) technology to solve a particular (health) problem, under ideal conditions of application.

## Effectiveness.

Probability that an individual benefits from the application of a technology to solve a particular problem, under real conditions of application.

Examples [from the healthcare sector]:

Highly effective treatments: vaccinations, heart surgery, diabetes, influenza, renal insufficiency, ...

Clinical interventions of known efficacy explain 5 of the years won in life expectancy at birth.

## Efficacy vs Effectiveness

In general, efficacy or ideal use or perfect use is the ability to produce a specifically desired effect. For example, an efficacious vaccine has the ability to prevent or cure a specific illness. In medicine a distinction is often drawn between efficacy and effectiveness or typical use. Whereas efficacy may be shown in clinical trials, effectiveness is demonstrated in practice.

The distinction between efficacy and effectiveness is important because doctors and patients often do not follow best practice in using a treatment. For instance, a patient using oral contraceptive pills to prevent pregnancy may sometimes forget to take a pill at the prescribed time; thus, while the perfect-use failure rate for this form of conception in the first year of use is just $0.3 \%$, the typical-use failure rate is $8 \%$.

## Illustration

$\star$ Clinical essay: efficacy of drug 1=75\%.
$\star \exists$ drug 2, same price and efficacy $=70 \%$
more effective to select drug 1 and reject drug 2?

YES, with this information.

## Additional INFO

- both drugs are correctly prescribed to $75 \%$ of patients
$\checkmark$ drug 1: 50\% of patients follow treatment correctly
- drug 2: 70\% of patients follow treatment correctly

Effectiveness of drugs:

$$
\begin{aligned}
& E_{1}=0.75 \times 0.75 \times 0.5=0.28125 \\
& E_{2}=0.7 \times 0.75 \times 0.7=0.3675
\end{aligned}
$$

Conclusion: select drug 2.

## Cost function

Cost function shows relationship between output and cost. $\rightarrow$ economic approach to production activity.

Def.: minimum possible cost of production of a given volume of output. (conveys efficiency)

Example: Let,
$q$ represent production of cars,
$L$ represent labor input (with price $w=1 €$ ),
$K$ represent capital input (with price $r=1.2 €$ ).

## We are assuming competitive markets!

Short run vs. long run: existence of fixed costs.
Total cost: $T C(q)=r K+w L=1.2 K+L$
Average cost: $A C(q)=\frac{T C(q)}{q}$
Marginal cost: $M C(q)=\frac{\partial T C(q)}{\partial q}$
Representation: Isocost map $\rightarrow K=\frac{\overline{T C}}{r}-\frac{w}{r} L$


To derive the total cost function, combine isocost map and isoquant map:

- To produce $q=100$ (i.e. 100 cars) given the prices $w$ and $r$, the factory minimizes cost by contracting 20 units of labor and 25 of capital. This yields a total cost of $T C(100)=(1.2) 25+20=$ $50 €$.
- To producte $q=150, \rightarrow T C(150)=(1.2) 40+$ $30=78$
- To producte $q=200, \rightarrow T C(200)=(1.2) 50+$ $45=105$




$$
A C(\tilde{q})=\operatorname{tg} \gamma=\frac{T C(\tilde{q})}{\tilde{q}} ; \quad M C(\tilde{q})=\operatorname{tg} \delta
$$

Remark 1: decreasing (long run) AC implies a range of values of $q$ such that $M C(q)<A C(q)$.

$$
\begin{aligned}
& \frac{\partial A C(q)}{\partial q}=\frac{\partial \frac{T C(q)}{q}}{\partial q}=\frac{M C(q) q-T C(q)}{q^{2}}= \\
& \frac{M C(q)}{q}-\frac{A C(q)}{q}<0 \Leftrightarrow M C(q)<A C(q)
\end{aligned}
$$

Remark 2: let $\hat{q}$ be such that $A C(\hat{q})$ is minimum. Then, $A C(\hat{q})=M C(\widehat{q})$.

If $A C(\hat{q})$ is minimum means derivative $=0$. Thus,

$$
\begin{aligned}
& \left.\frac{\partial A C(q)}{\partial q}\right|_{\overparen{q}}=\left.\frac{\partial \frac{T C(q)}{q}}{\partial q}\right|_{\widehat{q}}=\left.\frac{M C(q) q-T C(q)}{q^{2}}\right|_{\widehat{q}}= \\
& \left.\frac{M C(q)}{q}\right|_{\widehat{q}}-\left.\frac{A C(q)}{q}\right|_{\widehat{q}}=0 \Leftrightarrow M C(\hat{q})=A C(\widehat{q})
\end{aligned}
$$

## Economies of scale

Economies (diseconomies) of scale characterizes a production process in which an increase in the level of production causes a decrease (increase) in the long run average cost of each unit.


## Economies of scope

Economies of scope are changes in average costs because of changes in the mix of output between two or more products. This refers to the potential cost savings from joint production.

Consider a community with two hospitals. One specialized in pediatric care ( $q_{1}$ ), the other specialized in cancer care ( $q_{2}$ ). May it be worth to merge both activities in a single hospital?

Scope economies arise if

$$
T C\left(q_{1}, q_{2}\right)<T C\left(q_{1}\right)+T C\left(q_{2}\right)
$$

That is, the joint production of pediatric and cancer care allows for savings in the hospital's management structure, administration systems, management of hospital capacity, nurses, and non-sanitary personnel, etc.

## Opportunity cost.

The concept of opportunity cost is defined as the benefit given up by not choosing an alternative allocation.

Assume a shift from $B$ to $C$ (page 3b). Consequences?

- 29 additional units of hardware
- 29 less units of software.

The opportunity cost of moving from $B$ to $C$ is the reduction in production of software due to the increase in production of hardware.

The opportunity cost is an economic concept (not in accountancy).

How does society chooses among feasible allocations? VOTING mechanism.

Criteria to be used:

- Efficiency: Select only efficient allocations (rule out allocation $A$ )
- Equity. [Normative criterion] Select allocations meeting society's requirement for justice.
$\rightarrow$ people's values
e.g. social justice is behind the set-up of a NHS, public schools/housing.

Ł Horizontal and Verfical equity.
■ Horizontal equity: equal treatment of equal need.
$\square 2$ individuals with same profile should receive same treatment.

- Vertical equity: unequal treatment of unequal need. $\square$ preference for individuals with serious conditions (e.g. \# of kids) than for those with less serious conditions.
$\square$ passing the financing of NHS, public schools/housing to ability to pay (progressive income tax).


## Technical progress and its diffusion (see also Ch.5)

Technical progress: Defs.:
(a) produce "old" goods less costly, or produce "new" goods.
(b) Ability to produce at a lower cost given a quality level.

Diffusion: who adopts a new tech, and why.
2 principles:

- profit principle: firms more likely to adopt a new technique if it is expected to increase their revenue stream. [if present value of future profits due to innovation $>0$.]
- information principle: role of friends, colleagues, journals, and conferences at informing and encouraging the adoption decision.


## Trade-off:

- waiting may give rivals a competitive advantage;
- waiting allows for learning from others' experience.
(Classic) Pattern of diffusion
- Slow at the beginning;
- Then at an increasing rate;
- Then at a decreasing rate asymptotically reaching its limit $K$.

$(a, b)$ parameters to be estimated.

Individual vs. aggregate supply

## Individual supply $\rightarrow$ solution of

$$
\max _{x} \Pi(x)=x P_{x}-C(x)
$$

That is,

$$
x^{*}\left(P_{x}, w\right) \rightarrow \text { market structure? }
$$



NOTE: $P_{x}$ vs. $P(x)$.

Consider 2 firms $x_{1}\left(P_{x}, w\right)$ and $x_{2}\left(P_{x}, w\right)$.
The aggregate (market) supply for good $x$ is the horizontal sum of individual supplies.


## Effects on supply

Changes along the supply curve

- $\uparrow P_{x}, x \uparrow$ : some firms produce more and some others enter the market.
- $\downarrow P_{x}, x \downarrow$ : some firms produce less and some others leave the market.


Shifting the supply curve

- $\uparrow w$, ( $P_{x}$ constant), same productionj level is more expensive $\longrightarrow \downarrow$ production: supply moves inwards.
- R\&D $\longrightarrow$ more efficient technology $\longrightarrow$ same production level is cheaper $\longrightarrow$
$\uparrow$ production: supply moves outwards


## Illustration

Consider a firm with a production function $x(l)=$ $l^{\delta}$, where $l$ denote working hours and $x$ health services.

The associated cost function $C(w, x)=w l(x)$ where $l(x)=x^{1 / \delta}$, that is,

$$
C(x, w)=w x^{\frac{1}{\delta}}
$$

The (competitive) profit function is

$$
\Pi(x)=x P_{x}-C(x)
$$

The problem of the firm is to determine the level of $x$ to maximize profits. Formally,

$$
\begin{equation*}
\max _{x} x P_{x}-w x^{\frac{1}{\delta}} \tag{7}
\end{equation*}
$$

First order condition:

$$
\frac{\partial \Pi}{\partial x}=P_{x}-\frac{1}{\delta} w x^{\frac{1-\delta}{\delta}}=0
$$

Thus, the supply function of the firm is

$$
x\left(P_{x}, w\right)=\left(\frac{\delta P_{x}}{w}\right)^{\frac{\delta}{1-\delta}}
$$

Example Society with 2 (competitive) fims 1 and 2 and a good $x$.

$$
\begin{aligned}
& x_{1}(l)=l^{1 / 3} \\
& x_{2}(l)=l^{1 / 2}
\end{aligned}
$$

Individual supply functions:

$$
\begin{aligned}
& x_{1}\left(P_{x}, w\right)=\left(\frac{P_{x}}{3 w}\right)^{\frac{1}{2}} \\
& x_{2}\left(P_{x}, w\right)=\frac{P_{x}}{2 w}
\end{aligned}
$$

Aggregate supply:

$$
x\left(P_{x}, w\right)=\left(\frac{P_{x}}{3 w}\right)^{\frac{1}{2}}+\frac{P_{x}}{2 w}
$$

Elasticities

$$
\begin{aligned}
& \varepsilon_{x_{1}}=\frac{\partial x_{1}}{\partial P_{x}} \frac{P_{x}}{x_{1}}=\frac{1}{2} \\
& \varepsilon_{x_{2}}=\frac{\partial x_{2}}{\partial P_{x}} \frac{P_{x}}{x_{2}}=1
\end{aligned}
$$



## 3. The market

"Place" where consumers and producers interact (i.e. exchange goods).

What goods compose a market? $\rightarrow$ demand oriented vs supply oriented

Demand oriented: set of products with high crossed elasticities among them and low wrt other goods.

## Examples

(a) crossed elasticity between 95 octane and 98 octane gasoline is high. They are close substitutes. They belong to the same market.
(b) crossed elasticity between consumption of gasoline and mineral water is low. They are independent goods. They belong to different markets.

PROBLEM: ambiguity of high/low enough crossed elasticity.

## Supply oriented:

- Europe NACE (General Industrial Classification of Economic Activities [Nomenclature statistique des Activités économiques dans la Communauté Européenne]),
- Spain CNAE (Clasificación Nacional de Actividades Económicas)

PROBLEM: codes assigned according to technologically oriented criteria. May be misleading, e.g. elaboration of wine and champagne have different codes, but often grouped in the same market (high crossed demand elasticity).

Imperative assumption in the study of a market: Rational behavior of agents:

- consumers: maximize utility $\longrightarrow$ individual demand $\longrightarrow$ Market demand
- firms: maximize profits $\longrightarrow$ individual supply $\longrightarrow$ Market supply

Market structures:

| Sellers | Many | Few | One |
| :---: | :---: | :---: | :---: |
| Many | Perfect <br> Competition | Oligopsony | Monopsony |
| Few | Oligopoly | Bilateral <br> Oligopoly |  |
| One | Monopoly |  | Bilateral <br> Monopoly |

## PERFECTLY COMPETITIVE MARKET

 Justification:1. Simplicity.
2. Generates the best allocation of resources (no mismanagement): efficient distribution (Paretooptimality) [ $\neq$ equity].
3. No need of the State to achieve efficiency.
4. Benchmark to build models allowing better understanding of real phenomena.

## Assumptions:

1. Many sellers (producers): price-takers; given prices choose production volume to max profit.
2. Many buyers (consumers): price takers; given prices choose consumption bundle to max satisfaction.
3. Homogeneous product.
4. Perfect information.
5. Free entry (and exit) of firms.
6. Partial equilibrium. Static set-up.

Additional assumption:
7. Real markets (no financial markets)

- markets of goods and services: firms sell; consumers buy.
- labor markets: firms buy; consumers sell.


## Implicit assumption: property rights

8. Firms (shareholders) hold the property right over profits $\longrightarrow$ incentives to reinvest to improve profitability $\longrightarrow \Delta \Pi$.
9. Consumers hold the property rights over their incomes:

- incentives to work (increase income)
- incentivos to save (increase returns of capital)
$\Longrightarrow \Delta$ consumption.

A State setting incomes and profits eliminates incentives.

## Incentives

Are necessary but ... generate inequality.

Induce proper behavior if linked to profitability: higher profitability $\longrightarrow$ higher income.

Consequence: trade-off between incentives and inequality.

If society offers + incentives (e.g. $\nabla \mathrm{Tx}, \nabla$ social benefits) i.e. indiv. welfare. ~ income


If society offers - incentives (e.g. $\Delta T x, \Delta$ social benefits) i.e. indiv. welfare depends of income and social benefits

$$
\longrightarrow\left\{\begin{array}{l}
\nabla \text { production } \\
\nabla \text { inequality }
\end{array}\right.
$$

Societies solve the trade-off between the two forces through voting in government elections.

## Prices

allocate goods and services through the market to those with highest willingness to pay.

BUT is not the only allocation mechanism, e.g.
(i) Rationing (the consumption bundles consumers get are smaller that what they wish)

- por queuing (cinemas, primary care services, ...) $\longrightarrow$ inefficient
- por lotteries (licences, ...) $\longrightarrow$ inefficient
- por sharing rules (prorate shares in privatization of public firms, food stamp programs, wartime, ...)
- without market for coupons $\longrightarrow$ inefficient
- with market for coupons $\longrightarrow$ efficient
(ii) Fixing prices (gasolines, house-rental, ....)

Market equilibrium: Law of demand and supply.

Aggregate demand and supply of a commodity $x$ jointly determine its (partial) equilibrium price (and quantity) in a perfectly competitive market.

An equilibrium is a situation where no agent has incentives to modify his(her) actions.

The equilibrium pair $\left(P^{*}, x^{*}\right)$ denotes a situation where firms are maximizing profits and consumers are maximizing satisfaction from consumption.


## Ilustration

Recall the market demand in pp. $5 \mathrm{j}-5 \mathrm{k}$ and market supply in pp. 6k-6m.

$$
\begin{aligned}
& \text { Demand : } x^{D}\left(P_{x}, m\right)=\frac{m}{P_{x}} \\
& \text { Supply: } x^{S}\left(P_{x}, w\right)=\left(\frac{P_{x}}{3 w}\right)^{\frac{1}{2}}+\frac{P_{x}}{2 w}
\end{aligned}
$$

Assume $m=10$ and $w=1 / 3$, so that

$$
\begin{aligned}
\text { Demand : } x^{D}\left(P_{x}\right) & =\frac{10}{P_{x}} \\
\text { Supply : } x^{S}\left(P_{x}\right) & =P_{x}^{1 / 2}+\frac{3 P_{x}}{2}
\end{aligned}
$$

Equilibrium is characterized by $x^{D}\left(P_{x}\right)=x^{S}\left(P_{x}\right)$. Formally,

$$
\begin{aligned}
P_{x}^{1 / 2}+\frac{3 P_{x}}{2}=\frac{10}{P_{x}} & \Longleftrightarrow \\
\frac{3}{2} P_{x}^{2}+P_{x}-10 & =0
\end{aligned}
$$

That is, $P_{x} \approx 2.27$ and $x \approx 4.40$.


## Characterization of competitive equilibrium

- Firms (given prices) choose $q$ to maximize profits,
$\Pi(q)=p q-T C(q)$
$\frac{\partial \Pi(q)}{\partial q}=0 \rightarrow q^{*}$ s.t. $p=M C\left(q^{*}\right)$
- free entry guarantees zero profits, $\Pi\left(q^{*}\right)=0$
$\rightarrow p q^{*}=T C\left(q^{*}\right) \rightarrow p=T C\left(q^{*}\right) / q^{*}=A C\left(q^{*}\right)$.

Hence, at $q^{*}, p=M C\left(q^{*}\right)=A C\left(q^{*}\right)$.


Equivalence Max profits and Min costs

- Profit maximization:
$\max _{q} \Pi(q)=p q-w L-r K$ s.t. $q=f(K, L)$
Isoprofit map: $q=\frac{\bar{n}}{p}+\frac{w}{p} L+\frac{r}{p} K$
$\rightarrow$ optimum satisfies

$$
\frac{w}{p}=\frac{\partial f}{\partial L}, \text { and } \frac{r}{p}=\frac{\partial f}{\partial K} .
$$

Thus, profits are maximized at $\frac{w}{r}=\frac{\frac{\partial f}{\partial f}}{\frac{\partial f}{\partial K}}$.



## - Cost minimization:

$$
\min _{K, L} w L+r K \text { s.t. } q=f(K, L)
$$

Isocost map: $K=\frac{\overline{T C}}{r}-\frac{w}{r} L$
$\rightarrow$ optimum satisfies

$$
-\frac{w}{r}=-\frac{\frac{\partial f}{\partial L}}{\frac{\partial f}{\partial K}} .
$$

## Conclusion:

With given prices ( $p, r, w$ ), max profits $\Leftrightarrow$ min total cost. If a firm max profits producing $q^{*}$, it must be minimizing cost. Otherwise, it would mean there is a cheaper way to produce $q^{*}$ contradicting profit maximization.

## 4. Sources of market failure

## I. Supply side

(i) natural monopolies (scale economies) $\rightarrow$ large initial investment: supply of water, gas, electricity, transport, telecommunications, ...

Regulation (limit monopoly power) widely accepted (prices)
(ii) oligopolies (monopoly power) [see below]

Regulation (limit monopoly power): antitrust laws
(iii) Externalities $\rightarrow$ difficult to measure, diversity of effects, diversity of types. [see below]

Regulation (limit monopoly power): OK but how?
(iv) Merit goods and incomplete markets [see below]

## II. Demand side

(i) imperfect and incomplete information on products and markets.

Regulation: control on sales of dangerous products; info on label of products (expiry date, ingredients, ...); control on advertisement campaigns.
(ii) information as a public good* $\rightarrow$ private market does not provide enough information (see below).

Regulation: increase volume of information.

* public goods: no exclusion, no rivalry (public gardens, roads, army)


## OLIGOPOLY

Consider a market with two firms (duopoly) 1 and 2. Firm 1's decision will be affected by firm 2's behavior $\rightarrow$ Strategic interaction

## Firm 1's decision-making process

- Market price will depend on firms production levels: $P\left(x_{1}, x_{2}\right)$. Therefore,

1's profit maximization: find production level solving
$\max _{x_{1}} \Pi\left(x_{1}, x_{2}\right)=x_{1} P\left(x_{1}, x_{2}\right)-C\left(x_{1}\right)$
Solución: $x_{1}=f\left(x_{2}\right)$

Similarly, firm 2 maximizes profits producing
$x_{2}=g\left(x_{1}\right)$

## Market equilibrium

( $x_{1}^{*}, x_{2}^{*}$ ) such that $f\left(x_{2}\right)$ is compatible with $g\left(x_{1}\right)$



Formally, $\left(x_{1}^{*}, x_{2}^{*}\right)$ is a Nash (Cournot) equilibrium. That is,

$$
\pi_{i}\left(x_{i}^{*}, x_{j}^{*}\right) \geq \pi_{i}\left(x_{i}, x_{j}^{*}\right), \forall i, j i \neq j
$$

## MONOPOLY

## Profit maximization

$\max _{x} \Pi(x)=x P(x)-C(x)=R(x)-C(x)$
Marginal Revenue: $\Delta$ revenue when selling one additional unit

Marginal Cost: $\Delta$ cost when producing one additional unit

Average Cost: Total Cost/production (unit cost)
Firm's problem: $\max _{x} \Pi(x), \Longrightarrow M R=C M$


## Monopoly power

Monopolist: $p^{m}>M C=p^{c} \Rightarrow$ deadweightloss


Deadweightloss: Monopolist expels consumers unable to pay $p^{m} \rightarrow$ aggregate consumption $\downarrow\left(q^{c}-\right.$ $q^{m}$ ) Remaining consumers pay higher price. Consumer surplus $\downarrow$ upper yellow triangle.

Monopolist sells $q^{m}$ at higher price, but does not produce $\left(q^{c}-q^{m}\right)$ that could sell at a price $>M C \rightarrow$ Producer surplus $\downarrow$ lower yellow triangle.

Overall loss of efficiency: yellow triangle.

Regulation: may worsen situation if not adequate. BUT may improve situation if regulation is efficient.

Example: control on monopoly prices


Monopoly: $\left(P^{m}, q^{m}\right) \rightarrow$ welfare (deadweight) loss $=A B C$.

Government regulation: price cap $p^{r} \rightarrow q^{r} \rightarrow$ welfare (deadweight) loss $=F E C<A B C$.

Problem: Firm often multiproduct producer + demand and technology evolve $\rightarrow$ difficult to regulate properly.

Measuring monopoly power

- Firm level

Lerner index: $L_{i}=\frac{p_{i}-M C_{i}}{p_{i}} \in[0,1)$

- Aggregate level

$$
\mathcal{L}_{k}=\frac{\sum_{i=1}^{k} L_{i}}{k}
$$

$$
\mathcal{L}_{a}=\sum_{i=1}^{n} m_{i} L_{i}, m_{i}=\frac{q_{i}}{\sum_{i=1}^{n} q_{i}}
$$

$$
\mathcal{L}_{g}=\prod_{i=1}^{n}(L-I)^{m_{i}}, L_{i} \neq 0
$$

## 5. R\&D and technology transfer

## R\&D

- One of major use of funds by firms $\rightarrow$ develop new processes and/or products.
- Important element in competitive strategy of firms.
- Means to achieve an end.

Definitions

- Technology: "book" of specifications or blueprints of a process or product (engineering)
(i.e. something that if built/produced according to specifications will work).
$\rightarrow$ isoquant: technically efficient frontier of all possible techniques using the set of inputs.
$\rightarrow$ selection of technology according to relative prices of inputs (isocost).
- Innovation: first use of a new technology.
- Diffusion: spread of a (new) technology among users.
- Technological/product change: variation in the "book" of blueprints. Includes innovation and diffusion.
- Process innovation:
$\rightarrow$ shift isocost: no R\&D expenditure
$\rightarrow$ shift isoquant: outcome of R\&D investment.


## Elements in the R\&D expenditure decision



Total funds split in three uses:

- Market investment (advertising, ...)
- Physical investment (new plants, ...)
- R\&D investment


## R\&D investment

- 2 sources of uncertainty:
- prospective stream of expected returns in market (see below)
- likelihood of success, cost, and time span $\rightarrow$ project evaluation techniques.
- Expenses made on R\&D inputs (scientists, research facilities, materials)
- R\&D inputs "transformed" into R\&D outputs (patents, significant inventions) through R\&D "production function (black box).
- R\&D output subject to test of market profitability.


## Productivity of R\&D effort: related to

- (a) scale of operation
- (b) technological opportunities of sector
- (c) management of firm, R\&D unit, ...
(a) scale of operation
- indivisibilities in equipment $\rightarrow$ scale economies.
- pooling of risks of several projects $\rightarrow$ steadier flow of innovations $\rightarrow$ enables higher risk projects.
- parallel teams attraction for more and better researchers in better working conditions in wider array of projects.
(b) technological opportunities

Difficult to define. Proxies:

- distinction between science-based and traditional industries
- technological spillovers from R\&D efforts of other firms


## (c) management

- R\&D complex activity involving wide range of managerial, behavioral and sociological influences.
- e.g. decision of in-house and outsourcing projects.


## Market structure, capacity and incentives for R\&D

2 views:

- Schumpeter (1950): large firms are the main source of R\&D. They have more resources to invest and capital markets are imperfect (limiting borrowing capacity to small firms). Capacity argument
- Replacement effect: more competitive industries more incentives to mor R\&D investment. Incentives argument

- Assume process innovation allowing $\bar{c} \rightarrow \underline{c}$.
- Under monopoly, innovation is worth

$$
q^{m}(\bar{c}-\underline{c}) \equiv A
$$

- Under perfect competition, initially all firms use $\bar{c}$ and get $\pi_{i}=0$.
One firms obtains innovation $\rightarrow \tilde{p}=\bar{c}-\varepsilon$, captures
all market, and $\pi_{\text {innov }}=q^{c}(\bar{c}-\underline{c}) \equiv A+B$.
As initially, $\pi_{\text {innov }}=0, A+B=$ value of costreducing innovation, and $A+B>A$.

Why?
Monopolist's disincentive created by pre-innovation monopoly profits,
Competitiors' pre-innovation profits $=0$.

However, argument not fully consistent. Under perfect competition, innovator becomes an ex-post monopolist in the short-run.
In the long-run (after patent expiration), imitation $\pi_{i} \rightarrow$ 0.

Hence, optimal market structure: form of dynamic competition involving some degree of monopoly power in the short-run.

## Dynamics of R\&D competition

- Timing of innovation crucial in the market place.
- Innovation has winners and losers: first to innovate gets an advantage over rivals (due to patents).
- Rivalry in innovation $\Leftrightarrow$ race over time: firm devoting most resources in the shortest period of time is on average (because of uncertainty), winner of race.
- Fundamental asymmetry between firms in the R\&D race:
- some firms are patent-holders and/or incumbents in the market
-some other firms innovate to gain next patent and enter the market.

THUS, different firms have different incentives to win the patent race.

## Patent races

- Industry with 2 firms deciding whether to engage in R\&D.
- Investment of firm $k: i_{k}=\{0, I\}$.
- If $i_{k}=I$, innovation success with prob. $\alpha$.
- If $i_{k}=I$ value of innovation= $V$ if only successful; $V / 2$ if both successful; 0 if failure.
- $E \pi_{k}(n): k$ 's expected profit when $i_{k}=I$ and $n$ firms innovating ( $n=1,2$ ).
- Let $n=1$.

Then, firm 1 invests if $E \pi_{1}(1)=\alpha V-I \geq 0$.
That is, low success probability ( $\alpha$ ) or high R\&D cost $(I)$ yield no R\&D investment even under monopoly.

- Let $n=2$.

Then $E \pi_{k}(2)=\alpha(1-\alpha) V+\alpha^{2} \frac{V}{2}-I$.
Both firms invest if $E \pi_{k}(2) \geq 0 \Leftrightarrow \frac{\alpha(2-\alpha) V}{2} \geq I$.


## Socially optimal RD investment

From the society's viewpoint, $\triangle n$ increases probability of success, but also increases R\&D costs. $\rightarrow$ trade-off.

Let $E \pi^{s}(n)$ denote the industry (social) expected profits when $n$ firms do R\&D.

- If $n=1$, then $E \pi^{s}(1)=E \pi_{1}(1)$.

That is, when in equilibrium only one firm engages in R\&D, it is also socially optimal.

- If $n=2, E \pi^{s}(2)=2 \alpha(1-\alpha) V+\alpha^{2} V-2 I$.

Then, $E \pi^{s}(2) \geq E \pi^{s}(1) \Leftrightarrow \alpha(1-\alpha) V \geq I$.
Thus, for $n=2$ we distinguish 2 regions: $A$ and $B$.


- Region $A$ : Characterized by $E \pi^{s}(2)<E \pi^{s}(1)$ and $E \pi_{k}(2)>0$.
A relatively low R\&D cost makes it profitable for 2 firms to engage in R\&D.
However, the duplication of the R\&D cost offsets, from a social viewpoint, the benefits of the increased likelihood of success. This happens because individual firms do not take into account how their R\&D affect rival firms' profits.
- Region $B$ : Characterized by $E \pi^{s}(2)>E \pi^{s}(1)$ and $E \pi_{k}(2)>0$. Here R\&D cost are low enough for the benefits of increased probability of success offset the R\&D cost duplication.


## Expected date of discovery

Assume the race just described is repeated until one firm actually obtains the innovation. Let $E T(n)$ be the expected date at least one firm obtains the innovation when $n$ firms do R\&D.

- Let $n=1$. Then,
$E T(1)=\alpha+2 \alpha(1-\alpha)+3 \alpha(1-\alpha)^{2}+4 \alpha(1-\alpha)^{3}+\ldots$

$$
=\alpha \sum_{t=1}^{\infty} t(1-\alpha)^{t-1}=\frac{1}{\alpha} .
$$

- Let $n=2$. Then,

$$
\begin{aligned}
E T(2) & =\alpha(2-\alpha)+2 \alpha(2-\alpha)(1-\alpha)^{2}+ \\
& +3 \alpha(2-\alpha)(1-\alpha)^{4}+\ldots \\
& =2 \alpha(2-\alpha) \sum_{t=1}^{\infty} t(1-\alpha)^{2(t-1)}=\frac{1}{\alpha(2-\alpha)} .
\end{aligned}
$$

Note:

- $\frac{\partial E T(n)}{\partial \alpha}<0$. An $\uparrow$ in prob of success, shortens expected date of discovery.
- $E T(2)<E T(1)$. The more firms engage in R\&D, the shorter the expected date of discovery.

Cooperation in R\&D Antitrust legislation bans cooperation by firms in the final good markets. However, less clear in other dimensions.

Consider an economy with 2 firms deciding over investment i R\&D and output levels in a 2 -stage setup:

- stage 1: firms simultaneously decide R\&D investment;
- stage 2 : firms simultaneously decide output levels.

Let $q_{i}$ denote firm $i$ 's output level, and $x_{i}$ its investment in R\&D.

Assumptions

- Market demand: $p=100-\left(q_{1}+q_{2}\right)$,
- Production unit cost function:
$c_{i}\left(x_{1}, x_{2}\right)=50-x_{i}-\beta x_{j}, \beta>0$ [positive externality]
- R\&D cost function: $T C_{i}\left(x_{i}\right)=x_{i}^{2} / 2$.

Equilibrium concept: subgame perfect equilibrium

- Def.: An outcome is a SPE if it induces a Nash eq. in every subgame of the original game.

Solving methodology: backwards induction.

- take as given ( $x_{1}, x_{2}$ ) and solve stage $2 \rightarrow q_{i}^{*}\left(x_{i}, x_{j}\right)$
- plug-in $q_{i}^{*}\left(x_{i}, x_{j}\right)$ in $\pi_{i}\left(x_{1}, x_{2}\right)$ and solve stage 1 .


## Meaning of SPE

Firm $i$ when deciding $x_{i}$ (given its expectation on $x_{j}$ ), anticipates the consequences on its decision on $q_{i}$ (given its expectation on $q_{j}$ ).
stage 2

Given $\left(x_{1}, x_{2}\right)$, firm $i$ solves

$$
\max _{q_{i}} \pi_{i}\left(q_{i}, q_{j}\right)=q_{i}\left(100-q_{i}-q_{j}\right)-c_{i} q_{i}
$$

F.O.C.

$$
\frac{\partial \pi_{i}}{\partial q_{i}}=100-2 q_{i}-q_{j}-c_{i}=0
$$

Therefore,

$$
\begin{aligned}
q_{i}^{*}\left(x_{1}, x_{2}\right) & =\frac{1}{3}\left[100-2 c_{i}\left(x_{1}, x_{2}\right)+c_{j}\left(x_{1}, x_{2}\right)\right] \\
Q^{*}\left(x_{1}, x_{2}\right) & =\frac{1}{3}\left[200-c_{1}\left(x_{1}, x_{2}\right)-c_{2}\left(x_{1}, x_{2}\right)\right] \\
p & =\frac{1}{3}\left[100+c_{1}\left(x_{1}, x_{2}\right)+c_{2}\left(x_{1}, x_{2}\right)\right] \\
\pi_{i}^{*}\left(x_{1}, x_{2}\right) & =\frac{1}{9}\left[100-2 c_{1}\left(x_{1}, x_{2}\right)+c_{2}\left(x_{1}, x_{2}\right)\right]^{2}
\end{aligned}
$$

stage 1 Decision on R\&D investment. 2 alternatives

## - non cooperative

- cooperative


## Non-cooperative behavior

Firm $i$ solves,

$$
\begin{gathered}
\max _{x_{i}} \pi_{i}\left(x_{1}, x_{2}\right)=\frac{1}{9}\left[100-2\left(50-x_{i}-\beta x_{j}\right)+\right. \\
\left.\quad+\left(50-x_{j}-\beta x_{i}\right)\right]^{2}-\frac{x_{i}^{2}}{2} \\
=\frac{1}{9}\left[50+(2-\beta) x_{i}+(2 \beta-1) x_{j}\right]^{2}-\frac{x_{i}^{2}}{2}
\end{gathered}
$$

yielding,

$$
x_{1}^{n c}=x_{2}^{n c}=x^{n c}=\frac{100(2-\beta)}{9-2(2-\beta)(1+\beta)}
$$

Note,

- $x^{n c}>0$ if $\beta<2$.
$-\frac{\partial x^{n c}}{\partial \beta}<0: \uparrow$ means $\uparrow$ externality. Thus, firm $i$ has less incentives to invest in R\&D expecting to profit from investment of its rivals. Prisoner's dilemma $\rightarrow$ less investment than optimal.


## Cooperative behavior

Firms 1 and 2 solve

$$
\max _{x_{1}, x_{2}}\left(\pi_{1}+\pi_{2}\right)
$$

yielding,

$$
x_{1}^{c}=x_{2}^{c}=x^{c}=\frac{100(\beta+1)}{9-2(\beta+1)^{2}}
$$

Note,
$-x^{c}>0$ if $\beta<1.125$ (aprox.).
$-\frac{\partial x^{c}}{\partial \beta}>0$ : Incentives are aligned. The higher the externality the higher the higher the effort to profit from mutual externalities.
In turn, it implies $\pi_{1}^{c}+\pi_{2}^{c}>\pi_{1}^{n c}+\pi_{2}^{n c}$. Also, given the symmetry of the model, $\pi_{i}^{c}>\pi^{n c}, i=1,2$.

Cooperative vs noncooperative behavior Let $\beta \in(0,1.125)$. Then,
$x^{c}>x^{n c} \Leftrightarrow \beta>1 / 2$.
Also, $x^{c}>x^{n c} \Rightarrow Q^{c}>Q^{n c} \Rightarrow p^{c}<p^{n c}$.

## Patents

Def.: Legal right granted by Government giving the inventor the sole right to exploit the invention for a given period of time.

Patent: 2 social goals

- provide incentives to produce know-how,
- spread info about new discoveries as fast as possible (thus avoiding duplication of R\&D efforts).

An invention to be protected by a patent must be

- novel,
- non-trivial,
- useful.


## Effects of a patent

Distinguish

- during patent protection,
- close to patent expiration


## Innovation under patent protection

Patent protection grants monopoly power to manufacturer $\rightarrow$ pricing rule: $P=M C \Rightarrow$ deadweight loss wrt perfect competitive pricing.

$C S\left(P_{m}\right)=A P_{m} B$
$C S\left(P_{c}\right)=A P_{c} C=A P_{m} B+P_{m} P_{c} D B+D B C$
$\triangle C S=P_{m} P_{c} D B+D B C$, that is,
$\triangle C S$ transfer to firms $+\triangle C S$ deadweight loss
In addition to consider CS, discussions of welfare effects must consider change in deadweight loss before and after the protection.

## Innovation close to patent expiration

Argument: when patent expires, competition will lower prices $\rightarrow$ higher consumer surplus (proxy for social welfare)

$C S\left(P_{0}\right)=A P_{0} B$
$C S\left(P_{1}\right)=A P_{1} C=A P_{0} B+P_{0} P_{1} D B+D B C$
$\triangle C S=P_{0} P_{1} D B+D B C$, that is,
$\triangle C S$ from $\downarrow$ price $+\triangle C S$ from $\uparrow$ consumption

## Types of innovation

Consider a competitive economy with all firms using technology unit cost $c_{0}$.
In equilibrium, $p_{0}=c_{0}, Q_{0}$, and $\pi_{i}=0, \forall i$.
One innovator: $c<c_{0}$. As monopolist, max profits at $M R=c$. Let $p^{m}(c)$ denote monop. price for $c$.


Def.: Innovation is major if $p^{m}(c)<c_{0}$.
Let $c=c_{2}$. Innovator can undercut rivals charging monop. price for $c_{2}$.
Major innov. $\downarrow$ price and $\uparrow$ production $\left(Q_{2}>Q_{0}\right)$.

Def.: Innovation is minor if $p^{m}(c)>c_{0}$.
Let $c=c_{1}$. Innovator cannot exploit monop. power. It can only undercut with $p_{1}=c_{0}-\varepsilon$, captures all market $\left(Q_{0}\right)$, and $\pi_{i}=\left(c_{0}-c_{1}\right) Q_{0}>0$.

## Optimal duration of a patent

Fundamental issue in design of a patent system (US:
17 years; EU: 20 years)

To assess optimal value of $T$ consider 2-stage game:

- stage 1: Govt determines $T$,
- stage 2: innovator obtains patent during $T$ periods.

Consider a firm investing in R\&D to obtain a costreducing innovation.

Assumptions and notation

- Investment of $x$ yields innovation reducing firm's unit cost from $c>0$ to $c-x$,
- Cost of R\&D: $T C(x)=x^{2} / 2$,
- Innovation is minor (i.e. profit max price is $p=c$ ),
- Market demand: $p=a-Q, a>c$,
- Discount factor: $\rho \in(0,1)$,
- Innovator's present value of profits when investing $x$ in $t=1: \pi(x ; T)$.


Area $M=(a-c) x$ : innovator's profit gain.
Profit $M$ is enjoyed during $T$ periods. From $T+1$ on $\pi_{i}=0$.

Area $D L=x^{2} / 2$ : society's deadweight loss due to monopoly power held by innovator.
After $T$ price falls to $c-x$, production expands, and $\uparrow$ in $C S=M+D L$.

## Discounted present value (time value of money)

[money today is more valuable than money in the future by the amount of interest that money can earn.]

Compute the investment today at a return rate of $5 \%$, so that in three years we will receive 100 EUR:

$$
\begin{aligned}
& x(1.05)^{3}=100 \\
& x=\frac{100}{1.05^{3}}=86.383759
\end{aligned}
$$

In general, the present value of a capital $K$ to be payed in $n$ years at the interest rate $r$ is given by,

$$
x=\frac{K}{(1+r)^{n}}=\rho^{n} K
$$

where $\rho=1 /(1+r)$ is called the discount rate.

## Example:

-1 EUR at $r=5 \%$ in 10 years: $1.05^{10}=1.629$

- present value in 10 years of weight control:

$$
\frac{50}{1.629}=30.69
$$

- present value in 10 years of check-up:

$$
\frac{200}{1.629}=122.77
$$

Solving the game

Stage 2: The innovator's problem

Innovator decides $x$ to max present value of profits (recall profits after T are zero):

$$
\begin{aligned}
\max _{x} \pi(x ; T) & =\sum_{t=1}^{T} \rho^{t-1} M(x)-T C(x)= \\
& =\frac{1-\rho^{T}}{1-\rho}(a-c) x-\frac{x^{2}}{2}
\end{aligned}
$$

where $\rho=1 /(1+r)$.

The solution of this problem is

$$
x^{I}=\frac{1-\rho^{T}}{1-\rho}(a-c) .
$$

Note

$$
\frac{\partial x^{I}}{\partial T}>0, \frac{\partial x^{I}}{\partial \rho}>0, \frac{\partial x^{I}}{\partial a}>0, \frac{\partial x^{I}}{\partial c}<0 .
$$

## Stage 1: The government problem

Society's welfare is $M(x)$ during $T$ periods and $M(x)+$ $D L(x)$ from $T+1$ on. The planner's problem is,

$$
\begin{aligned}
& \max _{T} W(T)= \sum_{t=1}^{T} \rho^{t-1} M\left(x^{I}\right)+\sum_{T+1}^{\infty} \rho^{t-1} D L\left(x^{I}\right)- \\
& \quad \frac{\left(x^{I}\right)^{2}}{2}= \\
&= \frac{(a-c) x^{I}}{1-\rho}-\frac{\left(x^{I}\right)^{2}}{2} \frac{1-\rho^{T}}{1-\rho} .
\end{aligned}
$$

The solution of this problem, $T^{*}$, depends on the characteristics of the demand function, the production cost, and the cost of R\&D function.

We can prove the following (important) result: The optimal time span of a patent is finite, $T^{*}<\infty$. Compute,

$$
\begin{aligned}
W(1) & =\frac{(a-c)^{2}}{1-\rho}-\frac{(a-c)^{2}}{2} \\
W(\infty) & =\frac{(a-c)^{2}}{(1-\rho)^{2}}-\frac{(a-c)^{2}}{2(1-\rho)^{3}}
\end{aligned}
$$

and verify $W(1)>W(\infty)$.

## Transfer of technology

- Over $80 \%$ of patented inventions are licensed to other firms.
- 2 questions:
- why should an innovator be willing to give access to its innovation to a competitor?
- Elements in the license contract design? (see chapter 9)

Consider a 2-firm economy withy demand $p=a-$ $Q$. Initial technology, unit cost $c$, and R\&D cost is $T C(x)=x^{2} / 2$.

Assume firm 1 obtains a minor cost-reducing innovation, $c_{1}=c-x$.

Assume firm 1 charges firm 2 a per unit fee $\phi$ for every unit sold by firm 2.

How does firm 1 determines $\phi$ ?


- Fim 2's gain from using new tech $=c-(c-x)=x$.
- Therefore, if firm 1 sets $\phi=x$ will leave firm 2 indifferent between accepting or rejecting the contract. Assume, $\phi=x-\varepsilon$,
- Firm 2 faces cost $c_{2}=c-x-\phi \approx c$. Therefore, in equilibrium firm 2 does not change its production $q_{2} \rightarrow$ profits remains the same.
- However, firm 1 obtains all the surplus generated by new technology, $\pi_{1}\left(c_{1}, c\right)+q_{2}\left(c_{1}, c\right) \phi$.


## Summarizing

When firms decide production levels, welfare increases when the innovator licenses a minor cost-reducing discovery ( $Q$ remains unchanged $\rightarrow P$ remains unchanged $\rightarrow C S$ remains unchanges. Also, $\pi_{2}$ remains unchanged, but $\pi_{1}$ increases.

## 6. Externalities

A good shows externalities when it generates thirdparty effects outside the price system

- positive: vaccination of my neighbors on my chances to get infected, spillovers of R\&D, etc.
- negative: pollution, neighbor's loud music, etc.

Competitive market only considers private costs and benefits, not social ones $\rightarrow$ inefficiency: negative externalities $\rightarrow$ overproduction; positive externalities $\rightarrow$ underproduction.

Example: market of vaccination.
$D$ : demand (marginal private benefit)
$S$ : supply (marginal private cost)
$K$ : marginal external benefit
Initial situation: Competitive allocation $A . \rightarrow$ inefficient under positive externality $K$ :
marg. social benefit $=D+K>S=$ marg. social cost (=private social cost)

Government intervention: direct subsidy to producers of $K € \rightarrow$ supply shifts to $S^{\prime}=S-K$.

New equilibrium allocation: $q_{2}$ at price $p_{2} \rightarrow$ efficient.


## 7. Merit goods

Commodities that are "good" regardless of each individual's preferences: arts, compulsory education, compulsory social insurance, ...

Govt. regulation: promotion of their consumption.

## Incomplete markets $\bigcirc$ ○

Private insurers may not provide coverage for some illnesses: AIDS, cancer, ...

Govt. regulation: public provision of insurance, compulsory contracts on private insurers.

## 8. Uncertainty, Risk and Insurance

Individual: income $Y$, Utility $U(Y)$.
Two states: success, failure (prob. $p$ ) $\rightarrow Y_{s}, Y_{e}$
"Expected income": ex-ante average income weighted by $p$ : $E(Y)=p Y_{e}+(1-p) Y_{s}$
"Expected utility": ex-ante average utility weighted by $p$ : $E(U)=p U\left(Y_{e}\right)+(1 \diamond p) U\left(Y_{s}\right)$

Individual behavior facing probability of failure?
Distinguish Uncertainty and Risk
Def.: Risk
Individual can assign probabilities to the different states he may face.

Def.: Uncertainty
Probabilities of the different situations are exogenous.
example 1 (Risk): 2 lotteries

1. Careless driver:

Prob 1/10,000 $\rightarrow$ accident

Prob 9999/10,000 $\rightarrow$ no accident
2. Careful driver:

Prob 1/100,000 $\rightarrow$ accident

Prob 99,999/100,000 $\rightarrow$ no accident

Remarks

1. Driving style is a choice variable.
2. Occurrence of accident no proof of careless driving.
3. Occurrence of acccident is observable.

Example 2 (Uncertainty): 2 lotteries

1. Good researcher:

Prob $1 / 100 \rightarrow$ bad project
Prob 99/100 $\rightarrow$ good project
2. Worse researcher:

Prob 2/100 $\rightarrow$ bad project

Prob 98/100 $\rightarrow$ good project

## Remarks

1. "Researcher ability" is not choice variable.
2. Occurrence of bad project no proof of lack of ability.
3. Bad project is observable.

Three attitudes towards risk. Two alternatives: participate in a risky situation $\rightarrow E(U)$; do not participate $\rightarrow U(E(Y))$.

Def.: Risk aversion: $E(U)<U(E(Y))$.

Def.: Risk neutrality: $E(U)=U(E(Y))$.

Def.: Risk preference: $E(U)>U(E(Y))$.


## Example 1: tossing a coin

Individual: $Y=49 €, U(Y)=\sqrt{Y}$.

Alternative 1. Participate in a lottery: toss a coin.

If win $\rightarrow 98 €$. If loss $\rightarrow 0 €$.

Cost of participation: $49 €$.

Expected utility:

$$
\begin{array}{r}
E(U)=\frac{1}{2} U(49+98-49)+\frac{1}{2} U(49-49)= \\
\frac{1}{2} U(98)+\frac{1}{2} U(0) \approx 4.9497
\end{array}
$$

Alternative 2. Do not participate $\rightarrow U(49)=7$

Conclusion: $E(U)<U(E(Y))$. Risk averse individual decides not to participate.

Remark: $U(Y)$ is strictly concave.

How can the individual be induced to participate?

- $\triangle$ payment if winning: e.g. $256 €$

$$
\begin{aligned}
E(U)= & \frac{1}{2} U(49+256-49)+\frac{1}{2} U(49-49)= \\
& \frac{1}{2} U(256)+\frac{1}{2} U(0)= \\
& \frac{1}{2} 16=8>7
\end{aligned}
$$

$-\nabla$ participation cost: e.g. $24 €$

$$
\begin{aligned}
E(U)= & \frac{1}{2} U(49+98-24)+\frac{1}{2} U(49-24)= \\
& \frac{1}{2} U(147)+\frac{1}{2} U(25) \approx \\
& \frac{1}{2} 12.1243+\frac{1}{2} 5 \approx \\
& 6.0622+2.5 \approx 8.56232>7
\end{aligned}
$$

Remark: either way implies rising the expected value of the lottery. The seller of the lottery tickets would make a loss for sure if selling many tickets!

## Example 2: contracting insurance

Individual with assets valued $21000 €$.

Probability of losing $600 €=1 \%$

Probability distribution:

$$
\left\{\begin{array}{l}
1 \% \longrightarrow 15000 € \\
99 \% \longrightarrow 21000 €
\end{array}\right.
$$

Insurance: alter probability distribution

Insurance contract:

- indemnity $=6000 €$
- premium = $60 €$

New probability distribution:

$$
\left\{\begin{array}{l}
1 \% \rightarrow 20940 €(=21000-6000+6000-60) \\
99 \% \rightarrow 20940 €(=21000-60)
\end{array}\right.
$$

Equal wealth in both states of nature: Individual fully insured against loss.

Risk aversion $\rightarrow$ contract insurance.
$\star$ Demand of insurance
Recall:

- Individual: income $Y$, Utility $U(Y)$ concave.
- Two states: success, failure (prob. $p$ ) $\rightarrow Y_{h}, Y_{s}$
- $L$ loss of income if failure.
- Protection against loss $L \rightarrow$ insurance indemnity: $Z €$ when failure. Premium: $\alpha Z €$.

How much insurance to buy? (i.e. choose the value of $Z$ to $\max E(U)$ )

$$
\begin{aligned}
& Y_{s}(Z)=Y-L-\alpha Z+Z=Y-L+(1-\alpha) Z \\
& Y_{h}(Z)=Y-\alpha Z
\end{aligned}
$$

Formally,

$$
\max _{Z} E(U)=p U\left(Y_{s}\right)+(1-p) U\left(Y_{h}\right)
$$

Solution:

$$
\begin{aligned}
\frac{\partial E(U)}{\partial Z} & =\left.p \frac{\partial U}{\partial Y}\right|_{Y_{s}} \frac{\partial Y_{s}}{\partial Z}+\left.(1-p) \frac{\partial U}{\partial Y}\right|_{Y_{h}} \frac{\partial Y_{h}}{\partial Z} \\
& =\left.(1-\alpha) p \frac{\partial U}{\partial Y}\right|_{Y_{s}}-\left.\alpha(1-p) \frac{\partial U}{\partial Y}\right|_{Y_{h}}=0
\end{aligned}
$$

## Interpretation

Concave utility $\rightarrow$ decreasing marginal utility.
a Each extra euro of coverage implies higher income when failure. But expected marginal utility of each extra euro of coverage diminishes. Formally, $p \frac{\partial U}{\partial Y_{e}}(1-\alpha)$ diminishes as $Z$ increases (marginal benefit).

- Each extra euro of coverage implies higher cost (less income) when success. Thus, marginal income increases. Formally, $(1-p) \frac{\partial U}{\partial Y_{s}} \alpha$ increases as $Z$ increases (marginal cost).
© Combination of these two opposite effects determines optimal demand of insurance.


Highest premium willing to pay?

Def.: Certainty equivalent (CE). Level of income whose utility is equal to expected utility, $U(C E)=E(U)$.

Highest premium $=E(Y)-C E$


## $\star$ Supply of insurance

$Z^{*}$ depends on $\alpha$. In turn, $\alpha$ is a decision of insurance company. Such decision depends on the structure of insurance market.

Assumption: perfectly competitive market.

Expected profit = premia - indemnity payments

$$
E(B)=(1-p) \alpha Z-p(1-\alpha) Z=Z(\alpha-p)
$$

Problem: determine $\alpha$ solution of $E(B)=0 \rightarrow$ fair premium. Thus,

$$
\widehat{\alpha}=p
$$

## Interpretation

The fair premium is equal to the probability of failure. If insurer sets lower premium will incur (expected) losses. If insurer sets too a high premium will obtain (expected) extra profits $\rightarrow$ new entrants offering lower premia.
[Oligopoly: solve $\max _{\alpha} E(B)$ ]

ŁEquilibrium of the insurance market

- Demand: [marginal benefit = marginal cost]

$$
\left.p(1-\alpha) \frac{\partial U}{\partial Y}\right|_{Y_{s}}=\left.\alpha(1-p) \frac{\partial U}{\partial Y}\right|_{Y_{h}}
$$

- Supply

$$
\alpha=p
$$

Therefore, $p(1-\alpha)=\alpha(1-p)$, and market equilibrium is characterized by

$$
\left.\frac{\partial U}{\partial Y}\right|_{Y_{s}}=\left.\frac{\partial U}{\partial Y}\right|_{Y_{h}} .
$$

Equality only satisfied when $Y_{s}=Y_{h}$, i.e.

$$
\begin{aligned}
Y-L+(1-\alpha) Z & =Y-\alpha Z, \quad \text { or } \\
Z^{*} & =L .
\end{aligned}
$$

The individual optimally fully insured against expected loss.

## 9. Contract theory

## Introduction

So far, market failure $\rightarrow$ mkt power, $\Delta$ returns, public goods, externalities.

New element of analysis: private information (asymmetric, imperfect).

What is a contract?

- credible commitment between two parties specifying responsibilities and payments under all contingencies.
- Bilateral agreement: credible commitment s.t. contracting party (principal) delegates in contracted party (agent) decision making, against a payment.

Elements of a contract:
$\diamond$ Principal: offers contract; verifiable variables
$\diamond$ Agent: if accepts, performs effort for Principal.
Perfect agent: manager as perfect agent for the owner takes decisions (R\&D investment) "as if" (s)he would be the very owner taking decisions should (s)he have the same information as the manager.

- If there is no conflict, the agent behaves as if (s)he would be the principal rather than himself.
- If conflict of interest, problem for the principal: make sure that the agent (manager) respects the interest of the principal (owner).
- Usual scenario: conflict of interest between principal and agent.

Conflict of objectives:
© salary: income for agent, cost for principal

- effort: benefits principal, costly for agent


## INFORMATION?

Complete (perfect), incomplete (imperfect), symmetric (public), asymmetric (private)

## Definitions

Perfect information: at each move, party knows history of decisions so far.

Imperfect information: not perfect.

Complete information: every party knows all relevant information about other party.

Incomplete information: $\exists$ party uncertain about other party's behavior, i.e. there are random elements in the relationship.

Symmetric information: all parties have exactly the same information;

Asymmetric information: One party has more information than the other party.

## Illustration 1: complete information

2 firms deciding whether or not, investing in R\&D.

Payoff: profits.


Complete and perfect information


Complete and imperfect information

## Illustration 2: incomplete information

F1 may be aggressive (pr. $p$ ) or soft (pr. $(1-p)$ ). Nature determines. F2 does not know attitude F1.


Asymmetric info and conflict of objectives. Example

Owner (principal) contracts manager (agent) to defend interests of firm.
Owner cannot perfectly control manager's decisions.
Contract cannot be based on manager's behavior (not verifialble).
Owner does not have info on manager's characteristics.
Manager can exploit his informative advantage to his own benefit, instead of hospital's.

Aim: study relation between two individuals, where one of them has an informative advantage over the other and their objectives are not aligned. $\Longrightarrow$ Provision of incentives to reach objective. If interests would coincide, info would be communicated eliminating asymmetry.

3 topics:
moral hazard
adverse selection
signalling

## Moral hazard

In a moral hazard situation both parties have the same info at the moment of signing the contract, BUT afterwards the agent receives private info. The principal cannot observe (verify) the effort (action) exerted by the agent.


Examples

* labor contracts: publisher representative to sell books. Only verifiable element: \# books sold. Effort (\# hours visiting clients) not verifiable by publisher $\rightarrow$ payment cannot be dependent on effort.
$\star$ hospital: manager contracted to control costs. If fixed payment $\rightarrow$ insufficient effort.
$\star$ researchers: research center contracts researcher in a project. $\rightarrow$ difficult to distinguish a thinker from a dreamer. Fixed payment $\rightarrow$ little incentives to think.

Example 1. Public school with retrospective budget $\rightarrow$ little incentives for cost containment Naïve solution: prospective budgets.

Example 2. Fully insured driver $\rightarrow$ little incentive for careful driving.
Naïve solution: "bonus-malus" system

Example 3. Fully insured physician $\rightarrow$ little incentive to exert the (costly) efficient level of effort to obtain best diagnostic.
Naïve solution: make physician responsible for diagnostic errors. Reputation (cf. TV series "House")

Naïve solutions because too much risk on the agent: (i) public school may have high costs because unexpected $\triangle$ students, repair works ...(and for lack of effort)
(ii) driver may be unlucky on one occasion along the year.
(iii) physician may obtain a wrong diagnostic by accident.

Effect of a deductible

Assume insurance contains a deductible of $D €$ (Cost borne by insuree before insurer starts covering expenses). Individual compares the level of services obtained after paying the deductible ( $Q_{2}$ ) and without insurance $\left(Q_{1}\right)$.

## Example


$\star p$ : prob "accident"
$\star D=P_{1} Q_{1}$
$\star$ individual obtains $Q_{2}$ paying $D$
$\star$ benefit: area under demand curve between $Q_{2}$ and $Q_{1}$ (green area)

Insurer $\Delta D$ to $D^{\prime}=P_{1} Q_{3}$. Will the individual buy the insurance?

\& $\Delta$ payment if accident $=P_{1}\left(Q_{3}-Q_{2}\right)($ blue + yellow $)$
\& benefit: area under demand curve between $Q_{2}$ and $Q_{1}$ (blue+green)
\& Summary:

- expense increase:
- benefit increase: green

Conclusion:
If green $>$ yellow $\rightarrow$ contract insurance with deductible $D^{\prime}$.

Too a high deductible $\rightarrow$ eliminates incentives to contract insurance

## Effects of a copayment

Initial situation: no insurance $\left(P_{1}, Q_{1}\right)$
Contract insurance with copayment $c \in(0,1) \Rightarrow$ Demand increases $Q_{1} \rightarrow Q_{2}$


Value of services $=P_{1} Q_{2}$
$\Delta$ expenditure $=P_{1}\left(Q_{2}-Q_{1}\right)$ (blue+yellow)
$\Delta$ benefit $=$ area under demand curve between $Q_{2}$ and $Q_{1}$ (blue)
Triangle yellow: welfare loss $\rightarrow$ Individual demands more insurance services than optimum.

## Interpretation

Insurance $\rightarrow$ consumer "as if" ignorant real cost of health services $\rightarrow$ distortion in resource allocation between demand for insurance and other goods.

Copayment and market equilibrium

Initial situation: no insurance ( $P_{1}, Q_{1}$ ) with demand
= supply
Contract insurance with copayment $c \in(0,1) \Rightarrow$
Demand increases $Q_{1} \rightarrow Q_{2}$
New equilibrium: $\left(P_{2}, Q_{2}\right)$.

$\Delta$ expenditure $=P_{2} Q_{2}-P_{1} Q_{1}$ (blue + green + yellow) resource allocation distortion:
$\Delta$ benefit induced by copayment $=$ green
$\Delta$ costs additional demand $=$ blue
Deadweight loss from overproduction of insurance services = yellow

## Adverse selection

Adverse selection appears in situations where the agent has private information before signing the contract. In this case the principal can verify the agent's behavior. Principal knows there are several types of agents but cannot identify it at the moment of the contract.


Examples
$\star$ Insurance company may face a potential client with high or low risk. Insurer can design a contract for each type of insuree, but does not know ex-ante which is the optimal one.
$\star$ Regulation of a public monopoly. Theory: price to marginal cost and cover fixed cost with a transfer. $\rightarrow$ monopoly knows better its cost function than regulator. Regulator includes monopolist informational advantge in the design of the contract (transfer, price).

Asymmetric info may cause the market to perform poorly, and even disappear.

Asymmetric info, key element in insurance and health care markets.

Illustration: Akerlof's (1970) lemons market.

Used-cars on sale with $\neq$ qualities.
Sellers know about qualities better than buyers.
Lemons principle: Good cars are driven out of the market by the lemons

Simplified Akerlof's example (FGS, 2004, ch. 9):

- 9 used-cars qualities $=\left(0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1,1 \frac{1}{4}, 1 \frac{1}{2}, 1 \frac{3}{4}, 2\right)$
- Uniform prob. of picking a car $\left(=\frac{1}{9}\right)$
- Sellers know quality
- Buyers only know distr. qualities
- Reservation value to sellers= $1000 € /$ /unit quality
- Reservation value to buyers= 1500 €/unit quality
- Auctioneer calls out market prices
- Sale at a price s.t. $D=S$

Let $p=2000 €$ per car

- Supply:

Sellers willing to sell each car if for each car, price/unit $\mathrm{q} \equiv \hat{p} \geq 1000 \times q$ of car.
$\operatorname{car}(\mathrm{Q}=2) \rightarrow \hat{p}=\frac{2000}{2}=1000 € \rightarrow \mathrm{~S}=9$.

- Demand:

Average quality $=1$;
Buyers willing to buy if $p \leq 1500 \times 1=1500$;
(price)2000 $>1500$ (res.value) $\rightarrow D=0$.

## Let $p=1500 €$ per car

- Supply:

Sellers willing to sell each car if for each car, price/unit $\mathrm{q} \equiv \widehat{p} \geq 1000 \times q$ of car.
$\operatorname{car}(\mathrm{Q}=2) \rightarrow \frac{1500}{2}=750 €$ per unit of quality. $\operatorname{car}(\mathrm{Q}=1.75) \rightarrow \frac{1500}{1.75}=875 €$ per unit of quality. $\operatorname{car}(\mathrm{Q}=1.5) \rightarrow \frac{1500}{1.5}=1000 €$ per unit of quality.
$\rightarrow S=7$ cars; average quality $=3 / 4$.

- Demand:

Average quality=3/4;
Buyers willing to buy if $p \leq 1500 \times \frac{3}{4}=1125$; (price) $1500>1125$ (res.value) $\rightarrow D=0$.
etc, etc.

## Conclusion:

Under asymmetric info, $\exists p$ at which $D=S$.

Why? Lemons principle.

Assume symmetric info:

Buyers and sellers only know average quality ( $\bar{q}=$ 1).

Let $p=1500 €$ per car

- Supply:

Sellers willing to sell if $p \geq 1000 \times \bar{q}=1000$; (price)2000 $>1000$ (res.value) $\rightarrow S=9$.

- Demand:

Average quality $=1$;
Buyers willing to buy if $p \leq 1500 \times 1=1500$;
(price) $1500=1500$ (res.value) $\rightarrow D=9$.

Equilibrium price of $1500 €$ and 9 cars are sold.

## Adverse selection and the insurance market

Football player has more info on his real ability (value of his legs) than insurer.
Player insurance against (unknown) prob $p$ of injury.
If insurer ignores this fact, and sets premium according to average player statistics $\rightarrow$ losses. Why? - high risk (quality) players more interested in contracting insurance $\rightarrow$

- insurer's customers will be a biased population sample.

Insurers anticipates it $\rightarrow$ contracts with higher premia. Low risk (quality) players do not contract insurance: Exclusion

Conclusion: asymmetric info $\rightarrow$ inefficient resource allocation.
$\star$ ind. do not know their $p \rightarrow$ insurance against risk.
$\star$ If insurer offers same contract to everybody $\rightarrow$

- low risk indiv, too high premium $\rightarrow$ underinsurance
- high risk indiv, too low premium $\rightarrow$ overinsurance.


## Solutions

## Solution 1: Screening

Insurer offers menu of contracts:

- i) contract with high coverage and high premium;
- ii) contract with low coverage and low premium

Consequence: self-selection:

- low risk indiv, $\rightarrow$ contract ii)
- high risk indiv, $\rightarrow$ contract i).


## Problems

1. Argument OK if insurer is monopolist. A eq. if competition.
2. Even when $\exists$ eq, it is inefficient: low risk indiv. overinsured.

Solution 2: Signaling

## Signaling

Similar situation to adverse selection. After knowing his type and before signing the contract, the agent may send a signal observable by the principal.


Example
$\star$ Manager shows credentials (Ph.D., etc) as signal of ability when being contracted by owner. Also hangs from the walls of his office credentials so that owner and visitors can see them.

Alternatively, the principal may posses private info that transmits to the agent through the contract design.

| $\dagger$ |  | $\dagger$ | $\dagger$ | $\dagger$ | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Nature chooses } \\ & P^{\prime} \text { 's type } \end{aligned}$ | $P$ designs contract as signal | $\begin{aligned} & \text { A accepts } \\ & \text { or rejects } \end{aligned}$ | $\underset{\substack{\text { A exestrs } \\ \text { effort }}}{ }$ | $\begin{gathered} \text { Nature } \\ \text { plays } \end{gathered}$ | Outcomes <br> \& Paymen |
|  | Source: Macho-Stadler et al. (1994, p. 25) |  |  |  |  |

## Example

* University Dpts in job market include "goodies" in offers as signals of quality.

What is a signal? investment to disclose some info (the "type") yielding some advantage over keeping it secret.

## Solution 2: Signaling

Low risk indiv. willing to show they are low risk: e.g. volunteer medical reports.
$\Rightarrow$ Signaling theory

## Problem

high risk indiv. want to look like low risk imitating their signals.

## Consequence

- Insurers very cautions in interpreting signals
- As signaling is costly, low risk indiv. may prefer not to signal.


## Equilibria: 2 types

(i) Separating equilibrium
(ii) Pooling equilibrium

## (i) Separating equilibrium

Appears when signaling is very costly for high risk indiv. $\rightarrow$

- high risk indiv. do not imitate
- Insurer takes signals serously
- low risk indiv. obtain better contracts
- signaling attractive for low risk indiv.


## (ii) Pooling equilibrium

Appears when imitation is not very costly $\rightarrow$

- Insurer ignores signals
- Signals are useless
- Nobody signals


## Problem (technical, but important)

Even with high signaling costs, often also exist pooling equilibria.

Examples:

- Corporation places add looking for "young graduate" $\rightarrow$ education as a signal of ability
- Physicians' ability hard to know by patient.


## 10. Pricing

We already know:

- (perfectly) competitive markets: $p=M C$, $\pi_{i}=0 \forall i$, and Pareto-optimal with all surplus to consumers.
- Imperfectly competitive markets: $p>M C$, $\pi_{i}>0 \forall i$, surplus shared consumers/producers, but (efficiency) deadweight loss.

Is there a way to improve upon the deadweight loss induced by market power? YES if...

* firm gets info on individual demand characteristics (reservation prices, demand elasticities);

夫 no arbitrage opportunities in commodity transfers.

## THEN

Firms can adjust prices to profiles of (sets of) consumers $\rightarrow$ Price discrimination

## On arbitrage

2 types

- commodity transferability (low transaction costs):

Firm sells a commodity to a consumer at unit price $p$ and to another consumer at a (discriminated) price $q<p$. Then the latter can resell to the former at a price $p$ gaining $(p-q)$ per unit.

- demand transferability (self selection mechanisms): Firms sells a commodity in single units and in packs of two units at prices $p(1)$ and $p(2)$ respectively aiming at capturing the low and high demand consumers separately.


## Consequences:

- commodity transferability $\rightarrow$ eliminates price discrimination.
- demand transferability $\rightarrow$ favors price discrimination.


## Some examples

- turist vs. business class airplane tickets,
- kids vs. adults entrance tickets in amusement parks,
- fixed payment + variable payment in electricity bill, water supply bill, telephone calls, taxi rides, ...
- single ticket vs. multiple trips ticket in public transport

Definition of Price Discrimination

A firm price discriminates when the ratio of prices is different from the ratio of marginal costs for two goods offered by a firm. (Stigler, 1987).

In particular,
Price discrimination exists when sales of identical goods orservices are transacted at different prices from the same provider.

Price discrimination can also arise with product differentiation. For example, so-called "premium products" (capuccino compared to black coffee) have a price differential that is not explained by the cost of production.

# Taxonomy of price discrimination (Pigou, 1920) 

3 types according to the info producer has on consumer:

- First-degree (perfect) price discrimination: full info.
- Second-degree price discrimination: discrimination according to quantity demanded.
- Third-degree price discrimination: discrimination according to personal characteristics.

First degree (perfect) price discrimination
Producer knows the demand function of individual. It charges for every unit the consumer's willingness to pay $\rightarrow$ all surplus to producer.


Non-discr monop: $\left(q^{m}, p^{m}\right)$ and $\pi^{m}=$ area $\left[c p^{m} A B\right]$.
Also, $C S=$ area $\left[E p^{m} A\right]$.
Perfect discr monop: $p=$ willingness to pay between $[E, D]$ so that $\pi_{p d 1}^{m}=$ area $[E c D]$. Also, $C S=0$.

## Remarks

$\star[E c D]-\left(\left[E p^{m} A\right]+\left[c p^{m} A B\right]\right)=[A B D]>0 \rightarrow$
1st degree PD: yields

- $\triangle$ efficiency
- transfer of resources: consumers to producers.
$\star$ no costs associated to discrimination.

Second-degree price discrimination
Producer can associate consumers in $n$ groups according to $q$ purchased. Charges a different price to each group.
Consumers in group $k$ with reservation price $>p_{k}$ pay price $p_{k}, k=1, \ldots, n$


Producer announces price menu and consumers choose group (price). Self-selection mechanism.
Price policy also known as non-linear prices.
Some consumers within each group obtain some surplus.
All consumers can participate. No exclusion.
Examples: business vs. tourist class tickets. $2 \times 1$ sales; bundling.

## Third-degree price discrimination

Producer defines $n$ groups according to personal characteristics (age, gender,...).

Charges a different price to each group.
May involve exclusion of some consumers.


Examples: cheaper theater tickets for students. free access to public transport for children and elderly.

## Two illustrative examples

## Example 1:

$\star$ Monopolist facing 2 consumers $A$ and $B$.

* Monopolists produces a good at mg cost=3
$\star$ Consumers may buy 1 or 2 units of good.
* Reservation prices are:

|  | 1st unit | 2nd unit |
| :---: | :---: | :---: |
| A | 10 | 6 |
| B | 20 | 7 |

Benchmark 1: Perfect competition
$p^{c}=3, \pi=0, C S=7+3+17+4=31$,
$W=C S+P S=31$ maximum $(D L=0)$.

Benchmark 2; Nondiscr. monopolist
Monop. compares profits at each feasible price:

$$
\begin{aligned}
p=6 & \Pi=6 \times 4-12=12 \\
p=7 & \Pi=7 \times 3-9=12 \\
p=10 & \Pi=10 \times 2-6=14 \\
p=20 & \Pi=20 \times 1-3=17
\end{aligned}
$$

Therefore,
$p^{m}=20, \pi=17, C S=0, D L=14$.

First degree (perfect) price discrimination
Monopolist sells first unit to $A$ at $p_{1}^{A}=10$ and the second unit at $p_{2}^{A}=6$. Also, sells first unit to $B$ at $p_{1}^{B}=20$ and the second at $p_{2}^{B}=7$. Thus, $\pi=31, C S=0, W=31, D L \neq 0$.

Second-degree price discrimination[quantities] $p_{1}$ denotes price of 1 st unit, and $p_{2}$ price of 2 nd unit. Monopolist computes $\pi$ for every feasible ( $p_{1}, p_{2}$ ):

$$
\begin{aligned}
& \left(p_{1}, p_{2}\right)=(10,6) ; \pi=(2 \times 10)+(6 \times 2)-12=20 . \\
& \left(p_{1}, p_{2}\right)=(10,7) ; \pi=(2 \times 10)+(7 \times 1)-9=18 . \\
& \left(p_{1}, p_{2}\right)=(20,6) ; \pi=(1 \times 20)+(6 \times 1)-6=20 . \\
& \left(p_{1}, p_{2}\right)=(20,7) ; \pi=(1 \times 20)+(7 \times 1)-6=21 .
\end{aligned}
$$

Therefore,
$\left(p_{1}, p_{2}\right)=(20,7), \pi=21, C S=0, D L=10$.

## Third-degree price discrimination[consumers]

$p_{a}$ price to consumer $A$, and $p_{b}$ price to consumer $B$. Monopolist computes $\pi$ for every feasible ( $p_{a}, p_{b}$ ):

$$
\begin{gathered}
\left(p_{a}, p_{b}\right)=(6,7) ; \pi=(2 \times 6)+(2 \times 7)-12=14 \\
\left(p_{a}, p_{b}\right)=(6,20) ; \pi=(2 \times 6)+(1 \times 20)-9=23 \\
\left(p_{a}, p_{b}\right)=(10,7) ; \pi=(1 \times 10)+(2 \times 7)-9=15 \\
\left(p_{a}, p_{b}\right)=(10,20) ; \pi=(1 \times 10)+(1 \times 20)-6=24
\end{gathered}
$$

Therefore,
$\left(p_{a}, p_{b}\right)=(10,20), \pi=24, C S=0, D L=7$.
Remarks

1. Monopolist's ordering:

1st degree $>$ 3rd degree $>$ 2nd degree $>$ no-discr $>$ perf. compet

General: 1st degree best choice if feasible. Perf. compet. worst. Specific: 2nd and 3rd degree.
2. $C S=0$. General for 1 st degree. Specific for others.
3. $D L=0$. General for 1 st degree and perfect compet. $\rightarrow$ both equally efficient. Only appropriation of surplus.

## Example 2:

$\star$ Monop. produces cars, blue and red. $M C=10$.
$\star$ Consumers snobs and normal. $n$ of each type.
Each buys 1 unit.

* Reservation prices:

| Cons./car | Red | Blue |
| :---: | :---: | :---: |
| Snob | 25 | 20 |
| Normal | 22 | 20 |

Benchmark 1: Perfect competition
$p_{r}=p_{b}=10$. Produce $2 n$ red cars.
$C S=n(25-10)+n(22-10)=27 n, D L=0$.

Benchmark 2: Nondiscr. monopolist
Monopolist computes profits under alternative prices.
Then,
$p=22$. Produce $2 n$ red cars. $\pi=24 n$,
$C S_{\text {snobs }}=3 n, W=27 n, D L=0$.

First degree (perfect) price discrimination
Monopolist produces $2 n$ red cars. Sells them to snobs at $p_{r}^{s}=25$, and to normal at $p_{r}^{n}=22$. Thus, $\pi=27 n, D L=0$.

Second-degree price discrimination[quantities] Monopolist sells red cars at $p_{r}=25$ and blue cars at $p_{b}=20$. Then, $\pi=25 n, C S=0, D L=2 n$.

Third-degree price discrimination[consumers] Monopolist produces red cars only and sells them at $p_{r}^{s}=25$ and $p_{r}^{n}=22$. Then, $\pi=27 n, C S=$ $0, D L=0$.

Second-degree price discrimination. Analysis

Non-linear prices: depend on quantity $\rightarrow$ different average price.


$$
T=A+p q \quad \text { (2-part tariff) }
$$

A: entry fee to amusement park; access fee to telephone service, water supply, electricity supply, ... $p$ : price per unit of consumption

$$
T=p_{1} \widehat{q}+p_{2} \widetilde{q} \quad(2-\text { part tariff })
$$

- charge price $p_{1}$ to $q \in(0, \widehat{q})$
- charge price $p_{2}$ to demand beyond $\widehat{q}$.


## Illustration

Market with 2 consumers. Inverse demand functions:

$$
q_{i}(p)=\frac{\theta_{i}-p}{\theta_{i}}
$$

Monopolist: constant mg. cost (c), uses 2-part tariff $T=A+p q$.

Assume $c<\theta_{1}<\theta_{2}$ (participation constraint)

Monopolist's problem: determine $(A, p)$ to max. profits.

1. Aggregate demand:

$$
Q(p)= \begin{cases}\frac{\theta_{2}-p}{\theta_{2}} & \text { if } p>\theta_{1} \\ 2-p \frac{\theta_{1}+\theta_{2}}{\theta_{1} \theta_{2}} & \text { if } p \leq \theta_{1}\end{cases}
$$

2. Profit function:

$$
\pi(A, p)=2 A+(p-c)\left(2-p \frac{\theta_{1}+\theta_{2}}{\theta_{1} \theta_{2}}\right)
$$

3. Determination of $A$.

To max profits, monopolist has two instruments: $A, p$. Strategy: (a) extract all surplus from low willingness-to-pay consumer;
(b) extract max surplus from the other consumer with $p$.


$$
C S_{1}=\frac{\left(\theta_{1}-p\right)^{2}}{2 \theta_{1}}=A^{*}
$$

Then,
$\pi(A, p)=2\left(\frac{\left(\theta_{1}-p\right)^{2}}{2 \theta_{1}}\right)+(p-c)\left(2-p \frac{\theta_{1}+\theta_{2}}{\theta_{1} \theta_{2}}\right)$.
and

$$
p^{*}=\frac{c\left(\theta_{1}+\theta_{2}\right)}{2 \theta_{1}}(>c)
$$

## 2dPD vs. uniform price

* Producers' viewpoint

Discriminatory prices $\left(p_{1}, \ldots, p_{n}\right)$ yield higher profits than uniform price $\left(p^{*}\right)$


* Consumers' viewpoint

Consumer can choose between uniform price $p$, and 2-part tariff $T=A+(p-t) q$.


Consumers demanding less than $\gamma \rightarrow p$
Consumers demanding more than $\gamma \rightarrow T$
$\star$ Welfare
Consider a (representative) consumer:

- if $q<\gamma \rightarrow$ uniform price $p$
-if $q \leq \gamma \rightarrow$ 2-part tariff $T=p \widehat{q}+(p-t) \widetilde{q}$.


Initial situation: $\left(p, q_{0}\right)$
Change $p \rightarrow(p-t)$ implies $q_{0} \rightarrow q_{1}$.
Net welfare gain: $\triangle C S+\triangle P S$
$-\triangle C S=$ gaef

- $\triangle P S=$ behi - gabf (profit on new units - profits lost on old units)
Note:
- behi $>0$ if $p-t>c$
- gafb decreasing in $\gamma$.


## Third-degree price discrimination. Analysis

- Monopolist selling in $n$ markets (defined by e.g. personal characteristics, age, gender, education, income, ...)
- Monopolist produces single good with $C(Q)$.
- Demand in each market: $p_{i}\left(q_{i}\right), i=1, \ldots, n$.
- Monopolist's profit function

$$
\pi(q)=\sum_{i=1}^{n} q_{i} p_{i}\left(q_{i}\right)-C(Q)
$$

where $Q=\sum_{i} q_{i}$, and $q=\left(q_{1}, \ldots, q_{n}\right)$.

Monopolist's problem
Determine profit maximizing output volume in each market, i.e.

$$
\left(q_{1}^{*}, \ldots, q_{n}^{*}\right) \text { solution of } \max _{q} \pi(q)
$$

Solve system of FOCs:

$$
\begin{equation*}
\frac{\partial \pi(q)}{\partial q_{i}}=p_{i}+q_{i} \frac{\partial p_{i}\left(q_{i}\right)}{\partial q_{i}}-\frac{d C(Q)}{Q}=0, \forall i \tag{8}
\end{equation*}
$$

Solution: $\left(q_{1}^{*}, \ldots, q_{n}^{*}\right)$ s.t.
$M R_{1}\left(q_{1}\right)=\cdots=M R_{n}\left(q_{n}\right)=M C(Q)$.


Interpretation: Rewrite (8) as

$$
\begin{equation*}
p_{i}\left(1-\frac{1}{\varepsilon_{i}}\right)=p_{j}\left(1-\frac{1}{\varepsilon_{j}}\right)=M C(Q), \forall i, j ; i \neq j \tag{9}
\end{equation*}
$$

Hence, $p_{i}>p_{j} \Rightarrow \varepsilon_{i}<\varepsilon_{j}$. Monopolist exploits lower sensibility of demand to $\uparrow$ price.
Market power: rewrite (9) as

$$
\begin{equation*}
\frac{p_{i}-M C}{p_{i}}=\frac{1}{\varepsilon_{i}}, \forall i \tag{10}
\end{equation*}
$$

## Welfare aspects of 3dPD

Consider transition from uniform price $p^{u}$ to discriminatory prices $p=\left(p_{1}, \ldots, p_{n}\right)$.

## 2 potential effects:

(a) markets already covered with $p^{u}$, under $p \rightarrow$ $\uparrow \pi ; \downarrow C S ; \uparrow \downarrow Q_{\text {old }}$.
(b) $p$ may give access to new markets: $\uparrow \pi, \uparrow C S, \uparrow Q_{\text {new }}$.

In general, $p^{u} \rightarrow p$ conveys $\downarrow W$ except perhaps if $\uparrow Q$ under discrimination.

Thus, $\uparrow Q$ Nc condition for $\uparrow W$ under discrimination, but not sufficient.

## Ramsey prices

Consider a monopolist serving several markets. Produces a good with $C(Q)=F+c Q$.

Question: determine quantities (prices) in each market under the constraint of zero (economic) profits.

Examples:

- Pharma companies seeling drugs to several countries,
- (nonprofit) Hospital allocating laundry/catering/cleaning among services,
- (nonprofit) Research center allocating the cost of infrastructure among different projects.

Problem: Find Nc conditions for 2nd best efficiency.

$$
\begin{aligned}
& \max _{\left\{p_{i}\right\}} W(p)=\sum_{i}^{n}\left(C S_{i}+P S_{i}\right) \text { s.t. } \sum_{i}^{n}\left(p_{i}-M C\right) q_{i}=F \\
& \max _{\left\{p_{i}\right\}} L(p)=\sum_{i}^{n}\left(C S_{i}+P S_{i}\right)+\lambda\left(\sum_{i}^{n}\left(p_{i}-M C\right) q_{i}-F\right)
\end{aligned}
$$

Solution:

$$
\begin{equation*}
\frac{p_{i}-M C}{p_{i}}=\frac{\lambda}{1+\lambda} \frac{1}{\varepsilon_{i}} \tag{11}
\end{equation*}
$$

## Remarks

- All markets are served and fixed costs are covered
- Ramsey prices minimize welfare loss due to pricing above MC: more sensitive markets, smaller mark-up (i.e. minimize demand distortion).
- Complies with equity if lower income markets are associated with more elastic demands.


## Ramsey prices vs. 3dPD

Compare (10) and (11).

Rewrite (11) as

$$
\begin{equation*}
\frac{p_{i}-M C}{p_{i}}=(1-\mu) \frac{1}{\varepsilon_{i}}, \text { with } \mu=\frac{1}{1+\lambda} \in(0,1) . \tag{12}
\end{equation*}
$$

Rewrite (12) as

$$
\begin{equation*}
\mu p_{i}+(1-\mu) M R_{i}=M C \tag{13}
\end{equation*}
$$



Therefore, $p_{i}^{R} \leq p_{i}$.

## 11. Macroeconomics

## What is Macroeconomics about?

Global behavior of the economy. Aggregation.

Macro variables: GDP, Aggregate expenditure, Unemployment, Inflation, Consumption, Saving, Investment, Exports, Imports, Public expenditure, etc.

## Questions:

Long term growth,

Economic cycles,

Unemployment,

Inflation,

International Trade and Development,

Economic Policy (monetary, fiscal, labor, etc).

Definition of GDP: market value of all final goods and services produced within a country in a given period of time. ["Gross" means depreciation of capital stock included]

Measures of GDP: Two approaches: expenditure and income (equivalent)

GDP - expenditure: adding up expenditure on all final goods and services produced during the year.
$G D P=$ private consumption + investment

+ government spending + (exports - imports)

$$
\equiv C+G+I+(X-M)
$$

GDP - income: adding up all payments to owners of resources used to produce output during the year (aggregate income)

$$
G D P=W+P+(T-S)
$$

Equivalence in the National Income Accounts,

$$
W+P+(T-S)=G D P=C+G+I+(X-M)
$$

Private consumption (C): commodities and services acquired by households.

Investment (I): goods and services increasing the capital stock. Investment = Savings.

Public consumption (G): goods and services acquired by the public administrations (army, roads). No transfers (pensions, social programs) because these are transfers.

Net exports (X-M): net spending from rest of the world in goods and services yielding income to national producers.

Wages and salaries (W): Compensation of employees measures the total remuneration to employees for work done. It includes wages and salaries, as well as employer contributions to social security and other such programs.

Profits (P): Surplus due to owners of incorporated businesses. Often called profits.

Net taxes (T-S): Difference between the resources transferred from the families to the State and the transfers from the State to the families.

## Illustration:

real GDP components in Spain in 2006 (constant prices 2000)
Demand components

|  | $10^{6} €$ | $\%$ |
| :--- | ---: | ---: |
| Private consumption (C) | 553.867 | 56.7 |
| Public consumption (G) | 184.233 | 18.9 |
| Investment (I) | 298.362 | 30.6 |
| Exports | 254.985 | 26.1 |
| Imports | 315.258 | -32.3 |
| Net exports (X-M) | -60.273 |  |
| TOTAL | 976.189 | 100 |

Source: Contabilidad Nacional de España, INE.

Illustration (2):
real GDP components in Spain in 2006 (constant prices 2000)
Supply components

|  | $10^{6} €$ | $\%$ |
| :--- | ---: | ---: |
| Agriculture | 27.199 | 2.8 |
| Industry | 151.709 | 15.5 |
| Construction | 106.437 | 10.9 |
| Services | 583.773 | 59.8 |
| Net taxes | 107071 | 11.0 |
| TOTAL | 976.189 | 100 |

Source: Contabilidad Nacional de España, INE.

## Circular flow model:

Flow of resources, products, income, and revenue among economic decision makers.


## Legend:

Flows of income:
(1): GDP = Aggregate income.
(2): Taxes are transfers from families to the State.
(3): Transfers from the State to the families.
(4): Disposable income of families = Aggregate incometaxes+transfers.

Flows of expenses:
(5): Disposable income splits in consumption and savings (= investment).
(6): Investment adds to flow of expenditure.
(7): Public expenditure adds to flow of expenditure.
(8): Exports add to flow of expenditure from the rest of the world.
(9): Imports are transfers to the rest of the world.
(10): National account identity.

## Example

| Orange Inc. |  | Juice Inc. |  |
| :---: | :---: | :---: | :---: |
| Wages and salaries Taxes | $\begin{gathered} 15000 \\ 5000 \end{gathered}$ | Wages and salaries <br> Taxes <br> Purchase of oranges | $\begin{array}{r} 10000 \\ 2000 \\ 25000 \end{array}$ |
| Revenues from oranges Consumers Juice Inc. | $\begin{aligned} & 35000 \\ & 10000 \\ & 25000 \end{aligned}$ | Revenues from juice | 40000 |
| Profits before taxes Profits after taxes | $\begin{aligned} & 20000 \\ & 15000 \end{aligned}$ | Profits before taxes Profits after taxes | $\begin{aligned} & 5000 \\ & 3000 \end{aligned}$ |

## VA Orange Inc. = 35000 (revenues from oranges)

VA Juice Inc. $=40000-25000=15000$ (revenues from juice - cost of oranges)

VA total $=35000+15000=50000=$ GDP (production)

GDP (income): $10000+40000=50000$ (consumers expenditure)

GDP (income): $(15000+10000)+(20000+5000)=$ 50000 (wages + profits before taxes)

Total production $=$ Total income $=$ Total expenditure
real GDP and nominal GDP.
nominal GDP: market value of production at today's prices.

Example: Economy with two goods (apples and oranges)
$G D P n^{2006}=\left(P_{o r a}^{2006} * Q_{o r a}^{2006}\right)+\left(P_{a p p}^{2006} * Q_{a p p}^{2006}\right)$
Problem: If prices double, GDP also doubles $\Longrightarrow$ poor welfare indicator.
real GDP: market value of production at prices of a reference year (1996).
$G D P^{2006}=\left(P_{o r a}^{1996} * Q_{o r a}^{2006}\right)+\left(P_{a p p}^{1996} * Q_{a p p}^{2006}\right)$

## Illustration:

Evolution GDPn and GDPr Spain 1995-2003 (10 ${ }^{6}$ $€)$.

| Year | GDPn | price index | GDPr |
| :---: | :---: | :---: | :---: |
| 1995 | 437.783 | 100 | 437.783 |
| 1996 | 464.251 | 103.5 | 448.457 |
| 1997 | 494.140 | 105.9 | 466.513 |
| 1998 | 527.975 | 108.5 | 486.785 |
| 1999 | 565.419 | 111.4 | 507.346 |
| 2000 | 610.541 | 115.3 | 529.691 |
| 2001 | 653.927 | 120.1 | 544.496 |
| 2002 | 698.589 | 125.5 | 556.651 |
| 2003 | 744.754 | 130.5 | 570.556 |

Source: INE.

The working of the Economy
Model of aggregate demand and supply:
(1) understand incidence of the different forces on macro variables, and
(2) measure potential effectiveness of economic policies.

Aggregate demand is (the value of) the total quantity the different sectors of the economy are willing to spend in a particular period.

Graphically, market demand curve: relation between general price level of the economy and aggregate spending in goods and services in the economy.

Aggregate supply: (value of the) total quantity of goods and services firms in the country are willing to produce in a given period.

The market supply curve shows the production level firms are willing to supply at any given price level.

Macroeconomic equilibrium: characterization of the production level and of the price level.

Graphically: intersection point of aggregate demand and supply curves. Compatibility between consumers and producers behavior.

## Equilibrium: two (potential) problems

1. negative results: equilibrium price-production pair may not satisfy macro objectives (inflation, unemployment, investment level, ...)
2. unstable results: even if the economy reaches optimal equilibrium may be perturbed by external shocks. oil crisis, bird flu, ...

## $\Longrightarrow$ MACROECONOMIC POLICY

Aggregate supply and demand curves are shifted by changes in consumers and/or producers behavior (endogenous and/or exogenous shocks).

Options of the macroeconomic policy:

1. shift demand curve through fiscal and monetary policy;
2. shift supply curve through R\&D policies;
3. do nothing if the causes of the perturbation are not identified.



25-b

## Unemployment.

Objective: maximize employment level.

Active population: set of people legally able to work = employed + unemployed.

Activity rate: (employed/active pop.) ${ }^{*} 100$

Unemployment rate: (unemployed/employed)*100.

Labor market equilibrium: wage level inducing compatibility between labor supply and demand.

Full employment $\neq$ absence of unemployment $\longrightarrow$ frictional unemployment ( $3 \%-5 \%$ ).

Structural unemployment: lack of adjustment between labor demand and supply. (labor market rigidities, professional qualifications, ...)

Frictional + structural unemployment = involuntary unemployment = unemployment rate.

## Measuring Unemployment.

> "Encuesta de Población Activa" (Active population enquiry): estimated unemployment [harmonized across OECD countries].

Sampling on population $\longrightarrow$ number of employed, unemployed, discouraged, by age, sex, education level, length of unemployment, etc.

Def.: unemployed individual not working the previous week, but ready to take a job along the following two weeks.

Def.: employed individual with a job ( $\geq 1$ hour) in the previous week.

Active population $=$ population employed + population unemployed.

RESUMEN DE INDICADORES DEL MERCADO DE TRABAJO

(1) Segundo trimestre para la EPA y mes de agosto para las Afiliaciones y datos del SPEE.
(2) Porcentaje de activos sobre la población de 16 años y más. En las columnas fimales aparece la variación amual en puntos porcentuales.
(3) Porcentaje de ocupados a tiempo parcial sobre el total de ocupados. En las colummas finales aparece la variación amual en puntos porcentuales.
(4) Porcentaje de asalariados con contrato temporal. En las columnas fímales aparece la variación anual en puntos porcentuales.
(5) Porcentaje de parados sobre la población activa. En las columnas finales aparece la variación anual en puntos porcentuales.
(6) Porcentaje sobre el total de contratos. En las columnas finales aparece la variación anual en puntos porcentuales.

Fuente: INE (EPA) Y MTAS

EVOLUCIÓN DE LAS PRINCIPALES VARIABLES DE LA EPA. Datos corregidos *

|  | Variaciones interanuales |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | En miles |  | En porcentaje |  |
|  | $1^{\circ} \mathrm{Trim} 2005$ | $2^{\circ}$ Trim. 2005 | $1^{\circ}$ Trim. 2005 | $2^{\circ}$ Trim 2005 |
| Ambos sexos |  |  |  |  |
| Población de 16 años y más | 604,2 | 599,5 | 1,7 | 1,7 |
| Activos | 650,5 | 693,0 | 3,3 | 3,4 |
| - Ocupados | 760,3 | 897,1 | 4,3 | 5,0 |
| - Parados | -109,8 | -204,0 | -4,8 | -9,2 |
| Inactivos | -46,3 | -93,4 | -0,3 | -0,6 |
| Varones |  |  |  |  |
| Población de 16 años y más | 323,9 | 319,8 | 1,9 | 1,8 |
| Activos | 324,0 | 335,1 | 2,8 | 2,8 |
| - Ocupados | 370,8 | 396,3 | 3,4 | 3,6 |
| - Parados | -46,8 | -61,3 | -4,6 | -6,3 |
| Inactivos | -0,1 | -15,3 | 0,0 | -0,3 |
| Mujeres |  |  |  |  |
| Población de 16 años y más | 280,3 | 279,7 | 1,5 | 1,5 |
| Activas | 326,5 | 358,0 | 4,0 | 4,3 |
| - Ocupadas | 389,5 | 500,7 | 5,7 | 7,2 |
| - Paradas | -63,0 | -142,8 | -4,9 | -11,4 |
| Inactivas | -46,2 | $-78,1$ | -0,5 | -0,8 |
| Ocupados por ramas |  |  |  |  |
| Agricultura | -16,7 | 5,1 | -1,6 | 0,5 |
| - Industria | 30,1 | 8,6 | 0,9 | 0,3 |
| - Construcción | 175,9 | 168,0 | 8,1 | 7,5 |
| - Servicios | 571,0 | 715,4 | 5,1 | 6,2 |
| Ocupados por situación profesional y tipo de contrato |  |  |  |  |
| Trabajadores por cuenta propia | 31,1 | -60,8 | 1,0 | -1,9 |
| Asalariados | 678,3 | 907,5 | 4,7 | 6,2 |
| - Con contrato indefinido | 294,4 | 300,9 | 3,0 | 3,0 |
| - Con contrato temporal | 384,0 | 606,6 | 8,4 | 12,9 |
| Otros | 50,8 | 50,4 | 285,0 | 336,7 |
| Ocupados según jornada |  |  |  |  |
| A tiempo completo | 236,0 | 444,3 | 1,5 | 2,7 |
| - Varones | 242,6 | 291,2 | 2,3 | 2,7 |
| -Mujeres | -6,7 | 152,9 | -0,1 | 2,7 |
| A tiempo parcial | 524,3 | 452,9 | 34,5 | 28,6 |
| - Varones | 128,2 | 105,2 | 44,4 | 34,6 |
| -Mujeres | 396,1 | 347,6 | 32,1 | 27,1 |
| Tasa de actividad (1) <br> - Varones | 0,9 0,6 | 1,0 0,7 | - | - |
| - Mujeres | 1,1 | 1,2 | - | - |
| Tasa de paro (1) | -0,9 | -1,3 | - | - |
| - Varones <br> - Mujeres | $-0,6$ $-1,4$ | -0,7 $-2,3$ | $-$ | $-$ |

* Variaciones corregidas del impacto de los cambios en el cuestionario y método de entrevista calculado a partir de datos definitivos del primer trimestre
(1) Variaciones interanuales en puntos porcentuales.

Fuente: Elaboración propia a partir de INE (EPA).

## Inflation.

Sustained and generalized increase of the general level of prices of goods and services in an economy.

How to define that price level? $\rightarrow$ Two alternative price indices (weighted average of prices):

## 1. GDP deflator,

2. CPI (Consumer price index).

* GDP deflator

GDP deflator $=($ nominal GDP)/(real GDP).
In our economy with oranges and apples,
$G D P$ deflator $=\frac{\left(P_{a p p}^{2006} * Q_{a p p}^{2006}\right)+\left(P_{o r a}^{2006} * Q_{o \text { ora }}^{2006}\right)}{\left(P_{a p p}^{1996} * Q_{a p p}^{2006}\right)+\left(P_{o r a}^{196} * Q_{o r a}^{2006}\right)}$.
Comparison of a consumption bundle evaluated at today's prices and at the base year prices.

* Consumer Price Index.
$\mathrm{CPI}=$ nominal value of consumption bundle/real value of that consumption bundle.
consumption bundle: "Encuesta de Presupuestos Familiares del INE" $\rightarrow$ representative sample of consumption goods of families weighted by their importance.

CPI evolution: monthly, yearly, aggregated within the year, last 12 months.

Disaggregate CPI in sectorial price indices: nonenergy goods and services, energy goods and services, non-manipulated food, ... $\rightarrow$ analyze their evolution. (See sample figures)

## PRINCIPALES INDICADORES DE PRECIOS

Tasas de variación anual en $\%$

|  | Media amal |  |  | Dic. 03 | Dic. 04 | Ene. 05 | $\begin{gathered} \text { Mar. } \\ 05 \end{gathered}$ | $\begin{gathered} \text { Jun. } \\ 05 \end{gathered}$ | Ago. 05(2) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 03 | 04 | $05(1)$ |  |  |  |  |  |  |
| IPC: Total | 3,0 | 3,0 | 3,3 | 2,6 | 3,2 | 3,1 | 3,4 | 3,1 | 3,3 |
| IPSEBENE (3) | 2,9 | 2,7 | 2,7 | 2,5 | 2,9 | 2,8 | 2,9 | 2,5 | 2,4 |
| IPC sin alimentos ni energía | 2,9 | 2,4 | 2,4 | 2,5 | 2,6 | 2,5 | 2,6 | 2,4 | 2,4 |
| IPC no energético | 3,2 | 2,9 | 2,7 | 2,9 | 2,8 | 2,8 | 2,9 | 2,6 | 2,4 |
| IPC alimentación | 4,0 | 3,9 | 3,4 | 3,9 | 3,3 | 3,5 | 3,6 | 3,3 | 2,7 |
| - No elaborada | 6,0 | 4,6 | 3,0 | 6,4 | 1,8 | 2,3 | 2,9 | 3,4 | 2,7 |
| - Elaborada | 3,0 | 3,6 | 3,6 | 2,7 | 4,1 | 4,2 | 4,0 | 3,2 | 2,8 |
| IPC no alimentación | 2,7 | 2,7 | 3,2 | 2,2 | 3,2 | 2,9 | 3,3 | 3,1 | 3,5 |
| - Bienes industriales | 1,9 | 1,9 | 2,7 | 0,9 | 2,6 | 2,2 | 2,7 | 2,5 | 3,3 |
| - Energía | 1,4 | 4,8 | 8,7 | -0,1 | 7,6 | 6,0 | 8,2 | 8,2 | 11,5 |
| - Bienes industrial. sin energria | 2,0 | 0,9 | 0,9 | 1,2 | 1,2 | 1,0 | 1,0 | 0,8 | 0,7 |
| - Servicios totales | 3,7 | 3,7 | 3,8 | 3,6 | 3,8 | 3,8 | 4,0 | 3,7 | 3,7 |
| IPC manufacturas (4) | 2,4 | 1,9 | 1,9 | 1,7 | 2,2 | 2,2 | 2,1 | 1,7 | 1,5 |
| IPRI: Total | 1,4 | 3,4 | 4,7 | 1,1 | 5,0 | 4,8 | 5,1 | 4,4 | 4,6 |
| Bienes de consumo | 2,3 | 2,5 | 2,7 | 2,4 | 2,8 | 3,2 | 2,8 | 2,2 | 2,0 |
| - Alimentación | 2,1 | 3,8 | 1,8 | 3,1 | 2,9 | 3,2 | 2,0 | 0,8 | 0,7 |
| - No alimentación | 2,4 | 0,9 | 3,8 | 1,5 | 2,6 | 3,1 | 3,9 | 4,0 | 3,8 |
| Bienes de equipo | 1,2 | 1,5 | 2,0 | 1,3 | 1,6 | 1,8 | 2,0 | 2,1 | 1,9 |
| Bienes intermedios | 0,8 | 4,5 | 4,2 | 1,0 | 6,2 | 6,2 | 4,9 | 3,1 | 3,0 |
| Energía | 1,3 | 5,3 | 12,5 | -1,2 | 10,7 | 8,8 | 13,1 | 13,5 | 15,7 |
| IVU: Importación | -1,4 | 2,5 | 4,9 | -2,9 | 5,8 | 5,0 | 5,3 | 5,3 | 8,2 |
| - Bienes de consumo | 0,0 | 0,4 | 1,2 | -1,8 | 4,2 | 3,4 | 2,6 | 3,6 | 0,6 |
| Exportación | -1,5 | 1,0 | 4,3 | 0,1 | 2,2 | 5,1 | 4,8 | 3,2 | 5,7 |
| Precios percibidos por agricultores | 5,5 | 0,9 | 3,9 | 9,8 | 2,5 | 8,4 | 13,2 | -11,7 | - |
| Deflactor del PIB | 4,0 | 4,1 | 4,2 | - | - | - | - | - | - |

(1) Media del período del que se dispone de datos sobre igual período del año anterior. El dato del deflactor del PIB incluye el segundo trimestre.
(2) Los datos del IPRI y de los IVUS corresponden a julio.
(3) IPC general sin alimentación no elaborada y sin energía.
(4) Alimentos elaborados y bienes industriales no energéticos.

Fuentes: INE, MAPYA y SGAM.
(\%)
información disponible hasta mayo 1998


CPI and price index of non elaborated produced goods and services excluding fats, tobacco and touristic packs.
(\%)
Crecimiento acumulado en doce meses $\left(^{*}\right)$
información disponible hasta mayo 1998


Price index of non elaborated produced goods and services excluding fats and tobacco (BENE-X), and price index of services excluding touristic packs (SERV-T).

## CPI vs. GDP deflator

1. GDP deflator measures the prices of all goods and services produced.
CPI measures prices of goods and services in the representative consumption bundle.
2. GDP deflator considers only goods and services produced inside the country.
3. CPI is computed for a fixed consumption bundle; GDP deflator allows for variations of the bundle along time in accordance with the variation in the composition of the GDP.
4. CPI does not measure possibility of consumers to alter the composition of the bundle (neither substitution nor income effects.

Although CPI may differ from GDP, both convey the same info on the rhythm of price increase. See next figure.

## Illustration:



Source: US Department of Commerce, Department of Labor.

## The Phillips curve.

Inverse relationship between inflation rate and unemployment rate. Controversial!!!

Reductions of unemployment rate against increases in inflation rate;

If prices moderate their increment, will yield an increase in unemployment.


## The Natural Unemployment Rate

In the long term the economy tends towards an unemployment rate independent of the implementation of fiscal and/or monetary policies (with only short run effects).

## Illustration: US 1960-1995.



* 1960-1969: good fit (increasing inflation). Average inflation 2.5\%, unemployment 4.8\%
$\star$ 1970-1973: change in expectations (curve shifts). Average inflation and unemployment 5.2\%
- 1974-1983: oil shock. Worse fit. Average inflation 8.2\%, unemployment 7.5\%
- 1984-1995: improve expectations. Average inflation 3.7\%, unemployment 6.2\%

Controversy: curve shifts vs. existence of the curve.

## Macroeconomics of the health care market

## Variables: 4 groups

* population health status
- Life expectation at birth
- Mortality rate
- other: quality of life, morbidity, ...
$\star$ Life style and behavior
- consumption of tobacco, alcohol and other drugs
- other: education rate, ...
* Level of health services
- health expenditure per capita
- other: \% hospital and pharma expenditure, ...
* Health promotion
- \% health care over GDP
- other: number physicians, nurses, ...


## Relation between macro and health variables

$\star$ Economic growth
$\odot$ Positive effects on health:

- Life expectancy at birth: Spain 1960-97. $\triangle$ in 8 years (70 to 78 , both sexes)
- Child mortality rate: Spain 1975-1997.
$\diamond$ neonatal + postneonatal: $\nabla$ 21/1000 to 6/1000
$\diamond$ perinatal: $\nabla$ 19/1000 to $5 / 1000$
$\odot$ Negative effects on health:
- Suicide and selfinjuries rate: Spain 1960-97. $\triangle$ smooth since 1975
- tobacco consumption: Spain 1960-97. $\triangle 1000$ ciggarettes/inhab/year. $\rightarrow$
- Lung cancer mortality rate: $\triangle 21 / 10^{5}$ to $69 / 10^{5}$ (males)

Source: Corugedo et al. (1999, p. 273-276)
$\star$ Economic development and health expenditure Positive relation and more than proportional:

$\star$ Health expenditure and effects on health

Ambiguous effect. Decreasing returns of Health function $\rightarrow$

Initial stages of a health system, big impact; Mature health systems modest impact.

